

# Massive stars

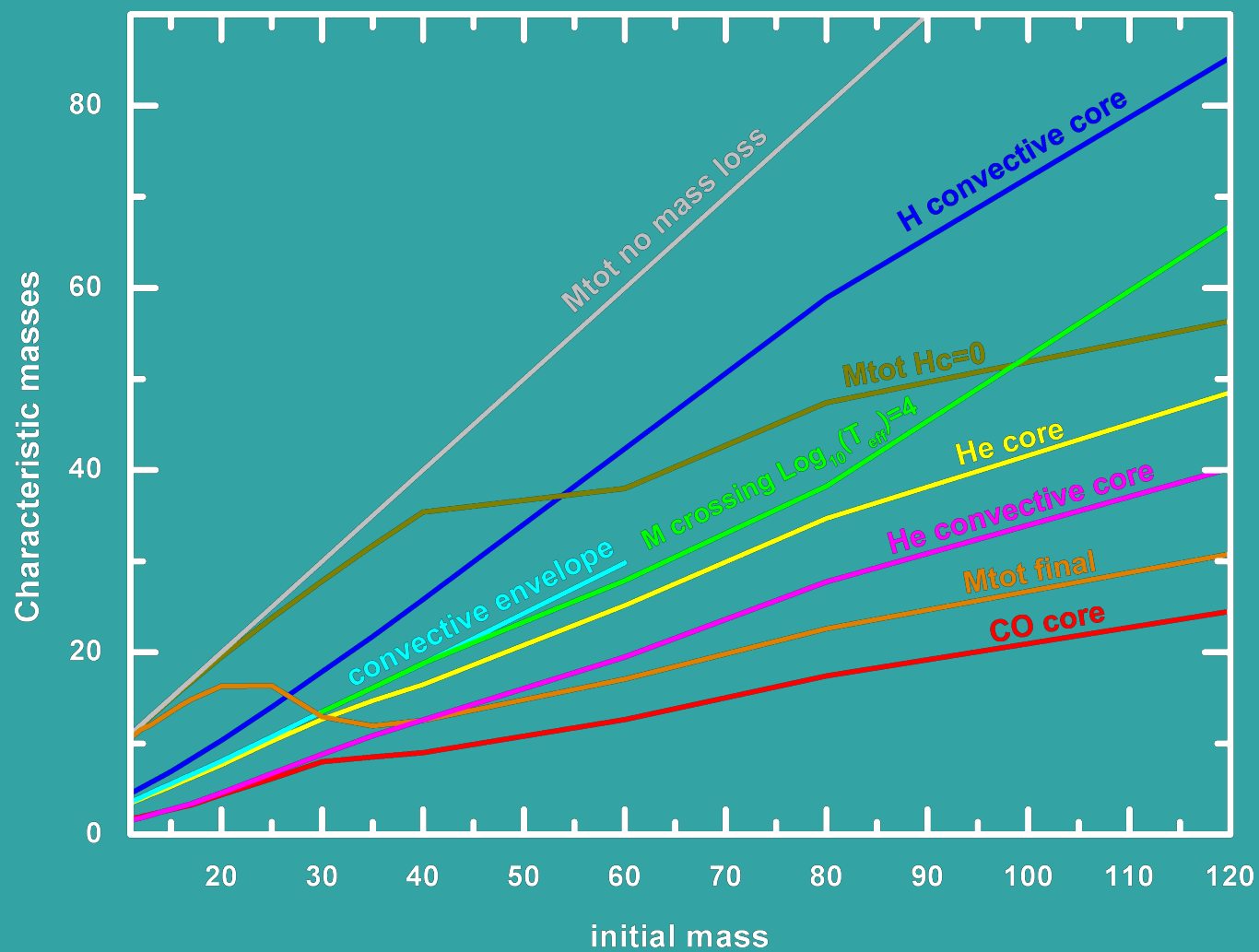
School on “The synthesis of the elements”

Granada (12-16 April 2010)

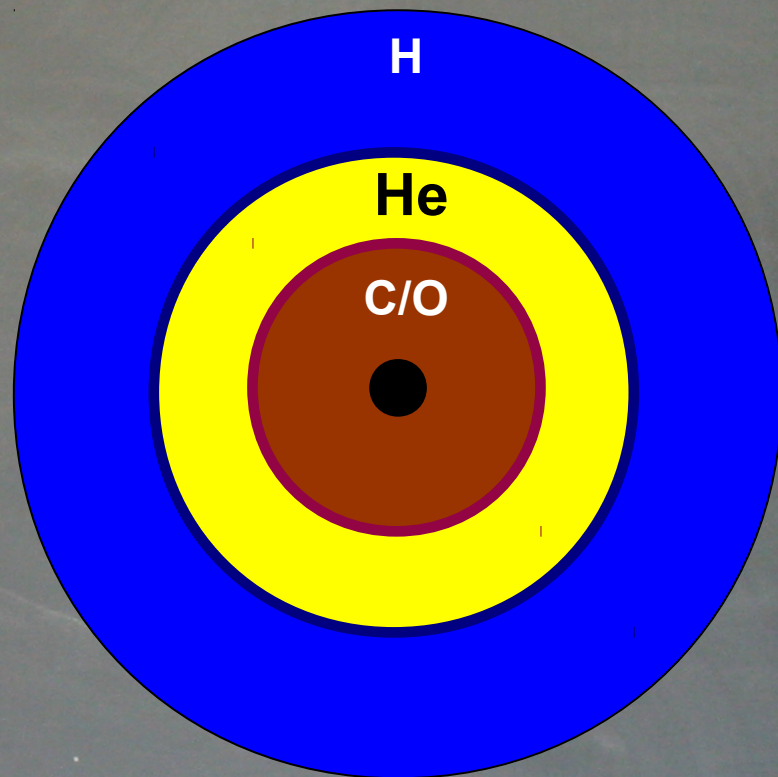
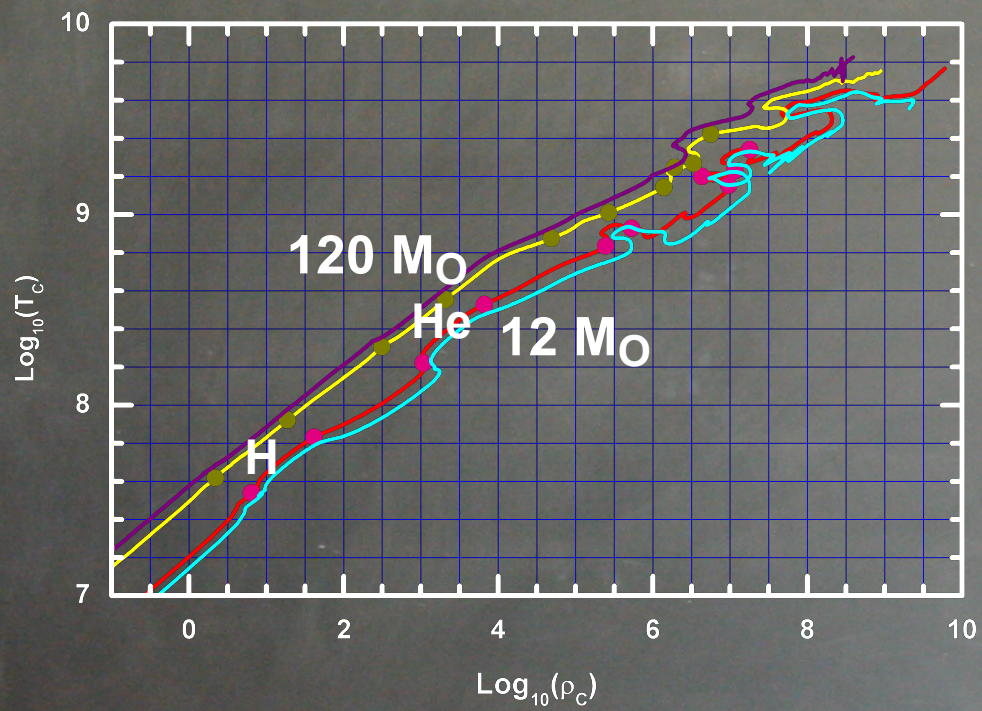
**Alessandro Chieffi**

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## Part 3









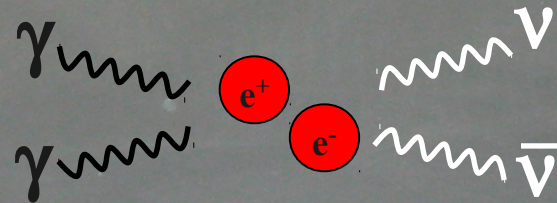
## Let's enter the advanced burnings...

The central temperature at the central He exhaustion is of the order of  $4 \cdot 10^8$  K and at roughly  $8 \cdot 10^8$  K the next fuel, carbon, starts burning.

But in the mean time....

...as the temperature increases, the peak of the Planck distribution moves towards higher energies and the number of photons having energy equal to 0.511 MeV (i.e. the mass of the electrons) increases dangerously.

When this happens,  $\gamma + \gamma$  begin to efficiently produce electrons-positron pairs.



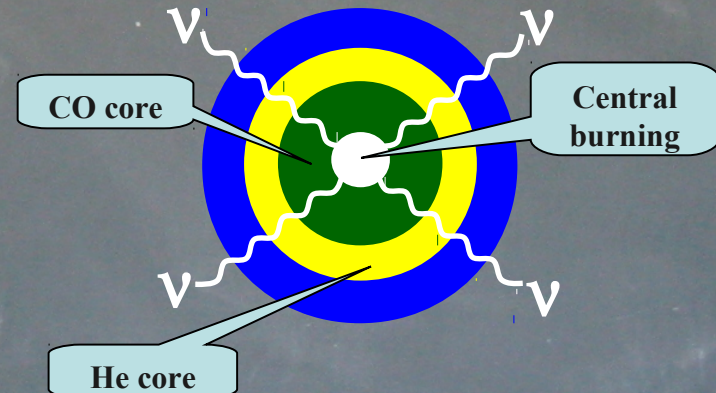
A blackbody radiation has its maximum wavelength at :  $\lambda_{\text{MAX}} = 2.898 \cdot 10^{-3} T^{-1} [\text{m} / \text{K}]$

BUT:

$$E = h\nu = hc/\lambda = hcT/(2.898 \cdot 10^{-3}) = 4.3 \cdot 10^{-10} T [\text{MeV}]$$

HENCE:

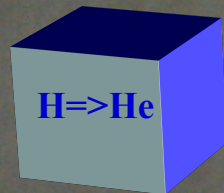
$$T = E / 4.3 \cdot 10^{-10} = 0.5 / 4.3 \cdot 10^{-10} \Rightarrow 1.15 \cdot 10^9 \text{ K}$$





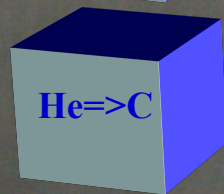
# Energy budget

$$t = E / L$$



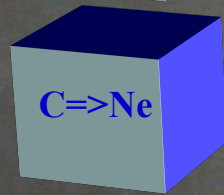
$6.44 \cdot 10^{18} \text{ erg gr}^{-1}$

$$t = 1.06 \cdot 10^{11} (L/L_0)^{-1} \text{ [yr / } M_{\odot}]$$



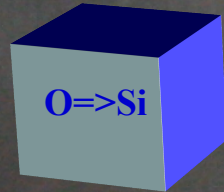
$5.84 \cdot 10^{17} \text{ erg gr}^{-1}$

$$t = 9.64 \cdot 10^9 (L/L_0)^{-1} \text{ [yr / } M_{\odot}]$$



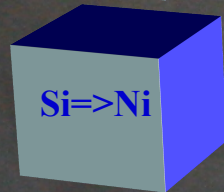
$1.85 \cdot 10^{17} \text{ erg gr}^{-1}$

$$t = 3.05 \cdot 10^9 (L/L_0)^{-1} \text{ [yr / } M_{\odot}]$$



$2.89 \cdot 10^{17} \text{ erg gr}^{-1}$

$$t = 4.77 \cdot 10^9 (L/L_0)^{-1} \text{ [yr / } M_{\odot}]$$

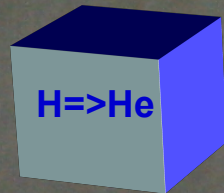


$1.88 \cdot 10^{17} \text{ erg gr}^{-1}$

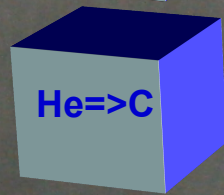
$$t = 3.10 \cdot 10^9 (L/L_0)^{-1} \text{ [yr / } M_{\odot}]$$



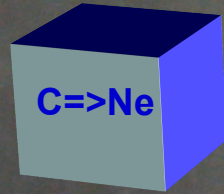
$$M=80 M_{\odot} \quad t = E / 10^6$$



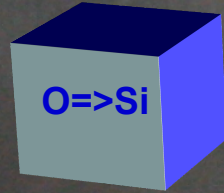
$$6.44 \cdot 10^{18} \text{ erg gr}^{-1}$$



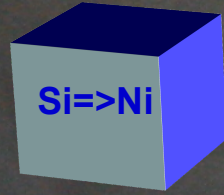
$$5.84 \cdot 10^{17} \text{ erg gr}^{-1}$$



$$1.85 \cdot 10^{17} \text{ erg gr}^{-1}$$



$$2.89 \cdot 10^{17} \text{ erg gr}^{-1}$$



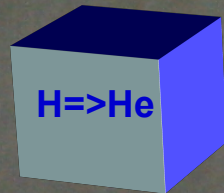
$$1.88 \cdot 10^{17} \text{ erg gr}^{-1}$$

L => total luminosity:  $L_{\gamma}$

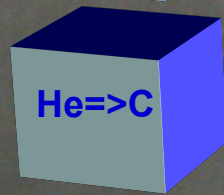
Mcc	Estimate d lifetime	Real lifetime	Revised lifetime	$L_{\text{TOT}}$
60	$6 \cdot 10^6$	$3.2 \cdot 10^6$		$10^6$
20	$2 \cdot 10^5$	$3.3 \cdot 10^5$		$10^6$
1.5	$4.5 \cdot 10^3$	$4.7 \cdot 10^2$		$10^6$
1	$4.8 \cdot 10^3$	$4.6 \cdot 10^2$		$10^6$
1	$3.1 \cdot 10^3$	$4.3 \cdot 10^3$		$10^6$



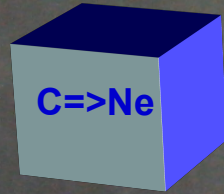
$$M=80 M_{\odot} \quad t = E / 10^6$$



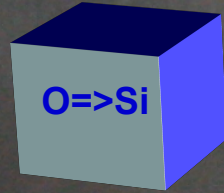
$$6.44 \cdot 10^{18} \text{ erg gr}^{-1}$$



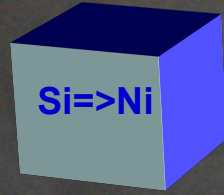
$$5.84 \cdot 10^{17} \text{ erg gr}^{-1}$$



$$1.85 \cdot 10^{17} \text{ erg gr}^{-1}$$



$$2.89 \cdot 10^{17} \text{ erg gr}^{-1}$$



$$1.88 \cdot 10^{17} \text{ erg gr}^{-1}$$

L => total luminosity:  $L_{\gamma} + L_{\nu}$

Mcc	Estimate d lifetime	Real lifetime	Revised lifetime	$L_{\text{TOT}}$
60	$6 \cdot 10^6$	$3.2 \cdot 10^6$		$10^6$
20	$2 \cdot 10^5$	$3.3 \cdot 10^5$		$10^6$
1.5	$4.5 \cdot 10^3$	$4.7 \cdot 10^2$	$4.5 \cdot 10^2$	$10^7$
1	$4.8 \cdot 10^3$	$4.6 \cdot 10^{-2}$	$4.8 \cdot 10^{-2}$	$10^{11}$
1	$3.1 \cdot 10^3$	$4.3 \cdot 10^{-3}$	$3.1 \cdot 10^{-3}$	$10^{12}$



# All the advanced phases are really neutrino dominated...

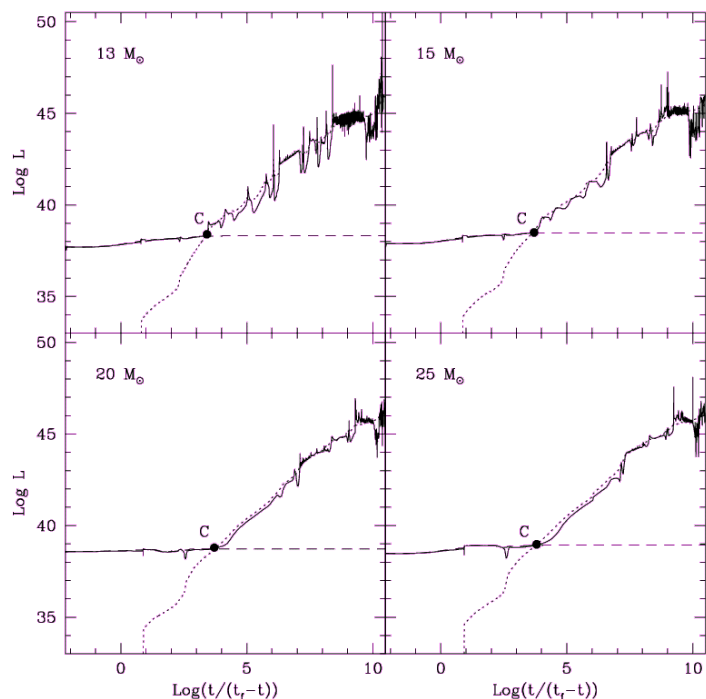
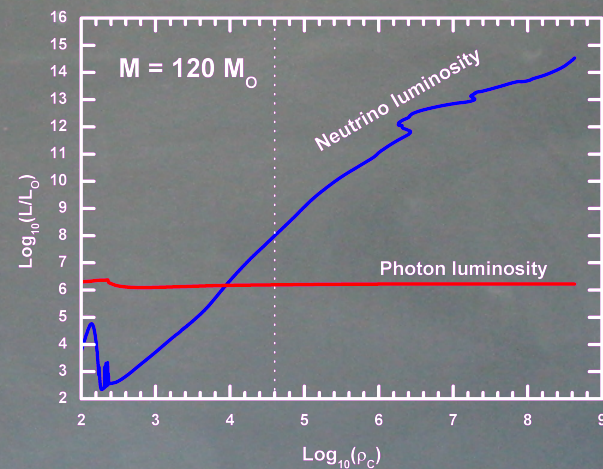
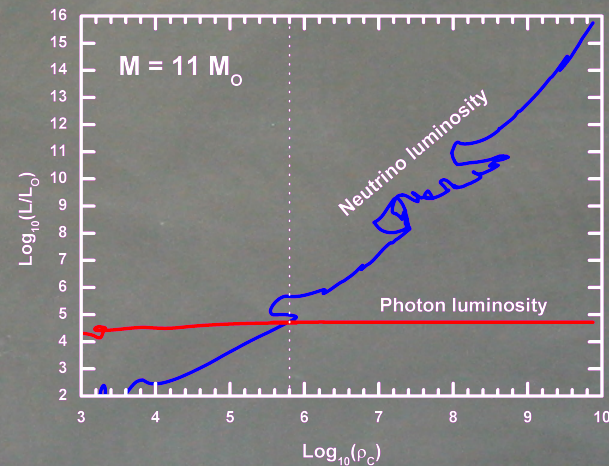
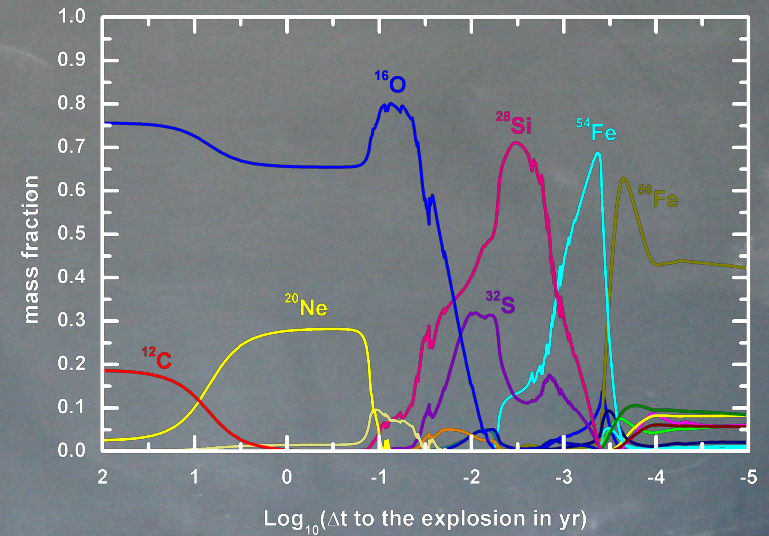
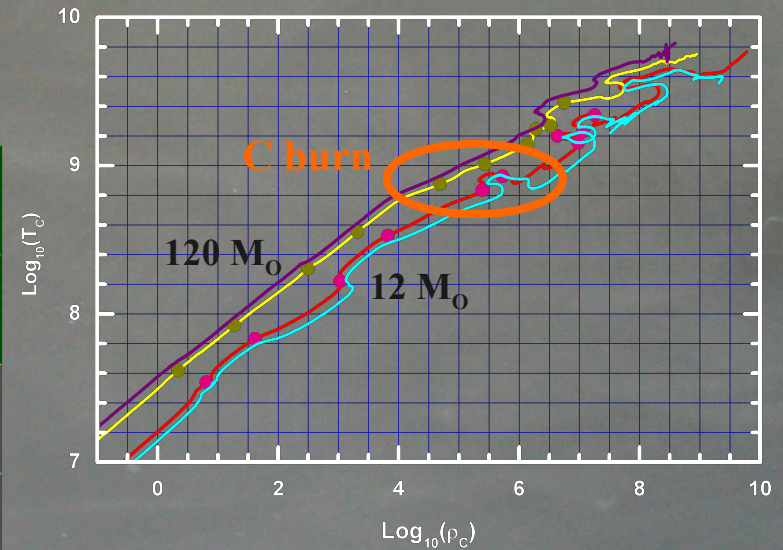
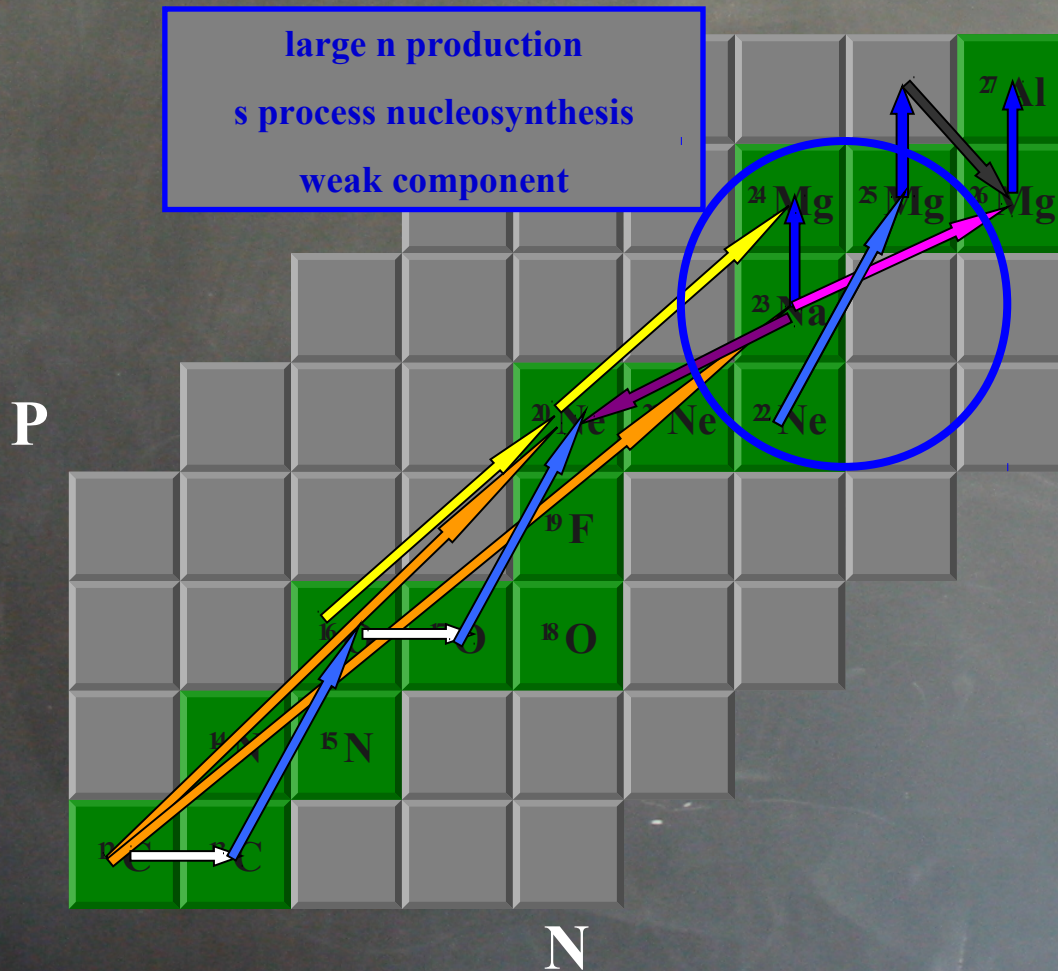


FIG. 7.—Temporal behavior of the various luminosities: photons (*dashed lines*), neutrinos (*dotted lines*), and nuclear (*solid lines*). The carbon-burning ignition is indicated in each panel by the big filled dot labeled "C."





**Typical temperature: 0.8-1.0 BK**

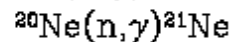
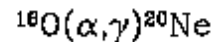
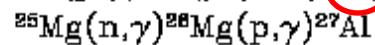
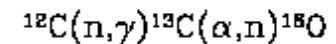
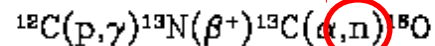
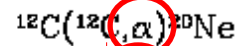




# Just the main processes in ...

## C burning

Panel a)



Panel b)

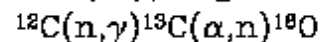
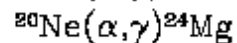
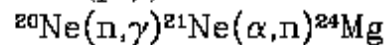
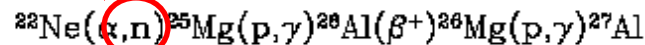
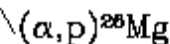
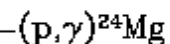
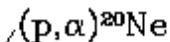
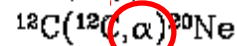
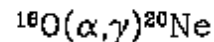


FIG. 6.—Most efficient nuclear processes during the central carbon burning. (a) The first part of the carbon burning; (b) the second part of carbon burning.



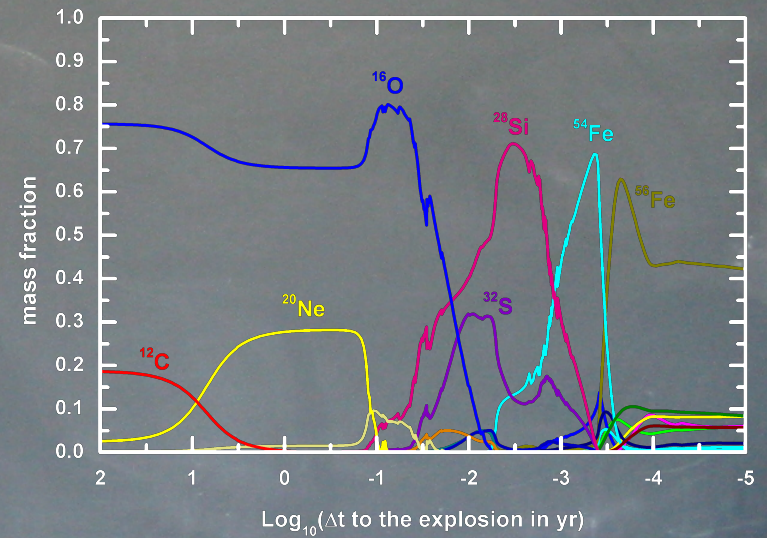
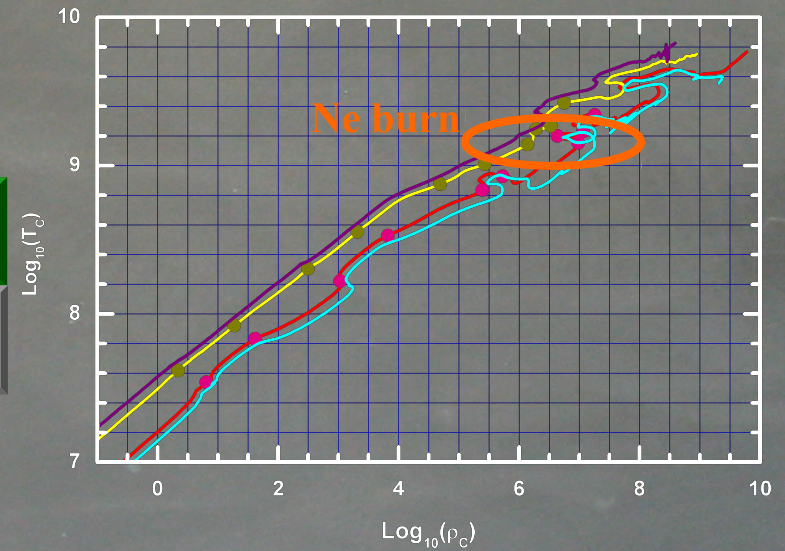
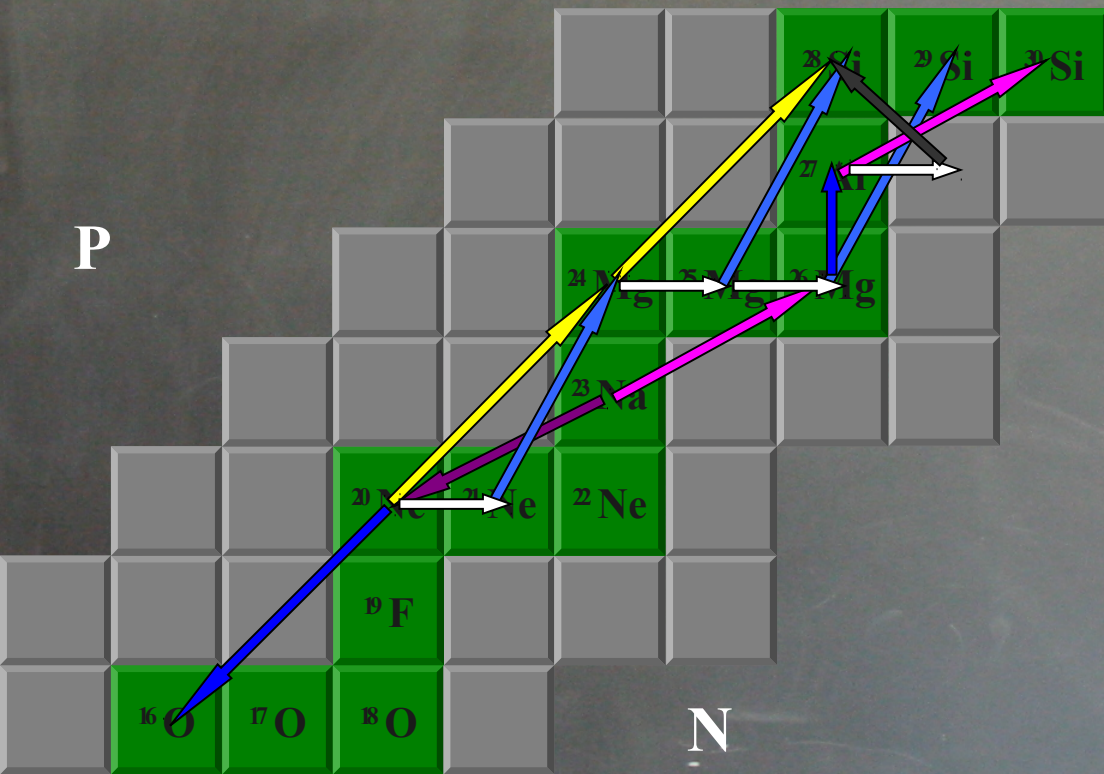
**Trailer time!**

**C burning movie**



# Ne burning

Typical temperature: 1.3-1.6 BK





# Just the main processes in ...

## Ne burning

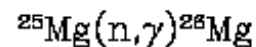
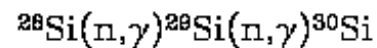
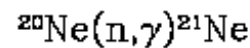
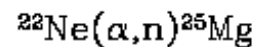
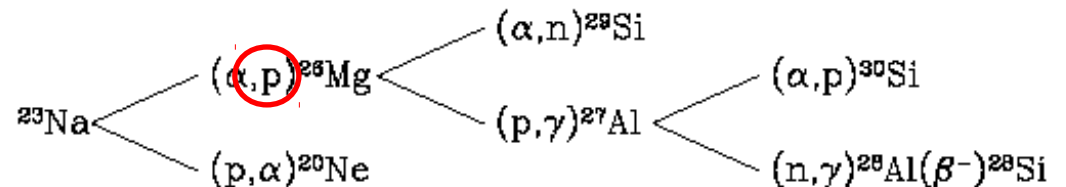
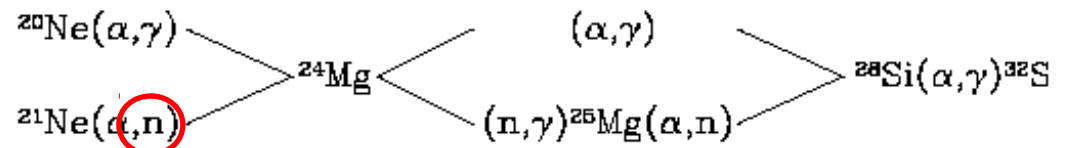
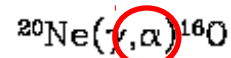


FIG. 8.—Most efficient nuclear processes during the central neon burning



**Trailer time!**

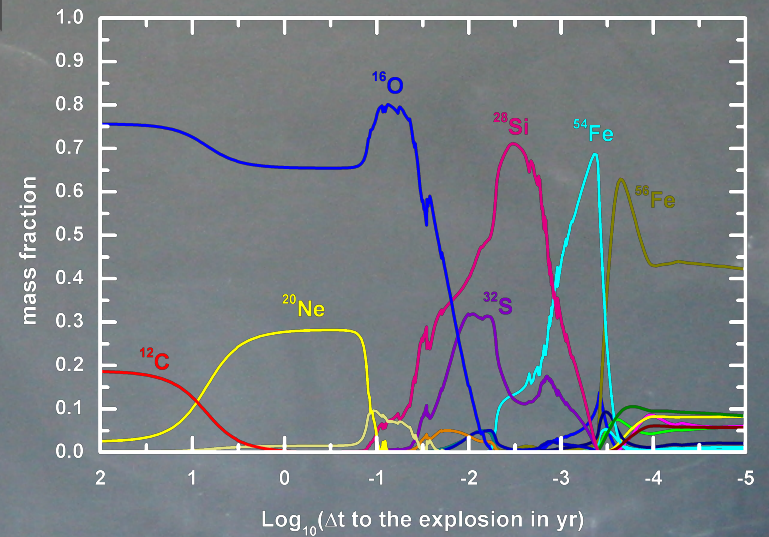
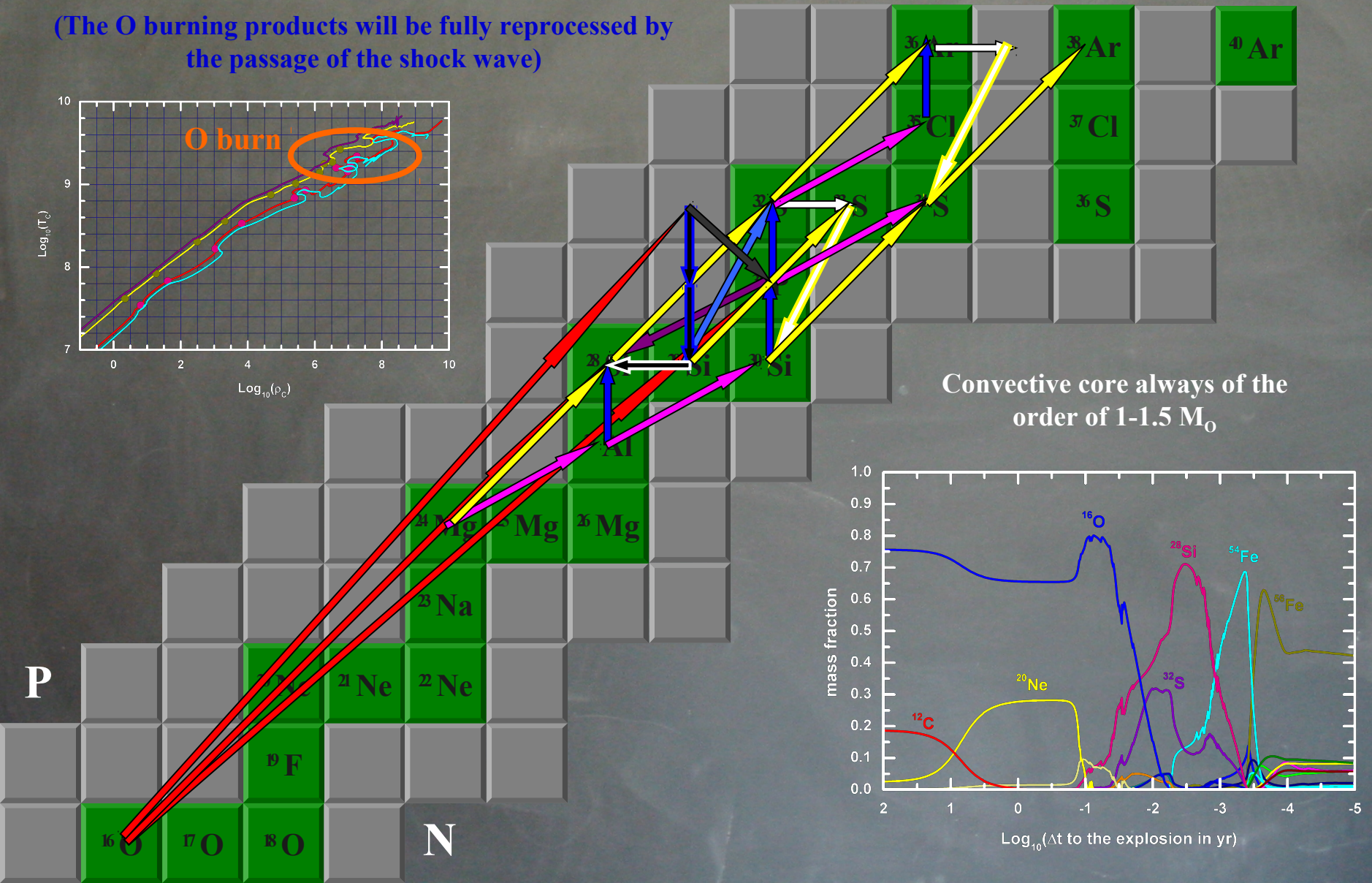
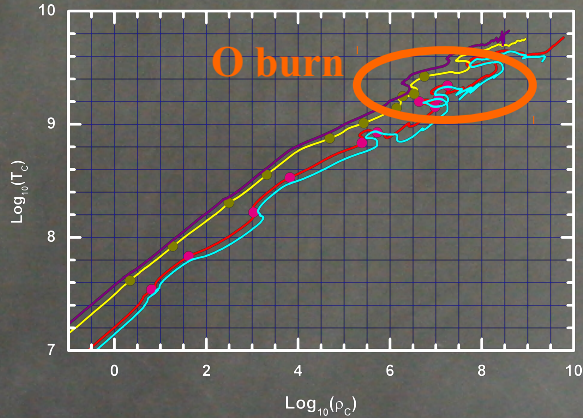
**Ne burning movie**



# O burning

Typical temperature: 2.-2.5 BK

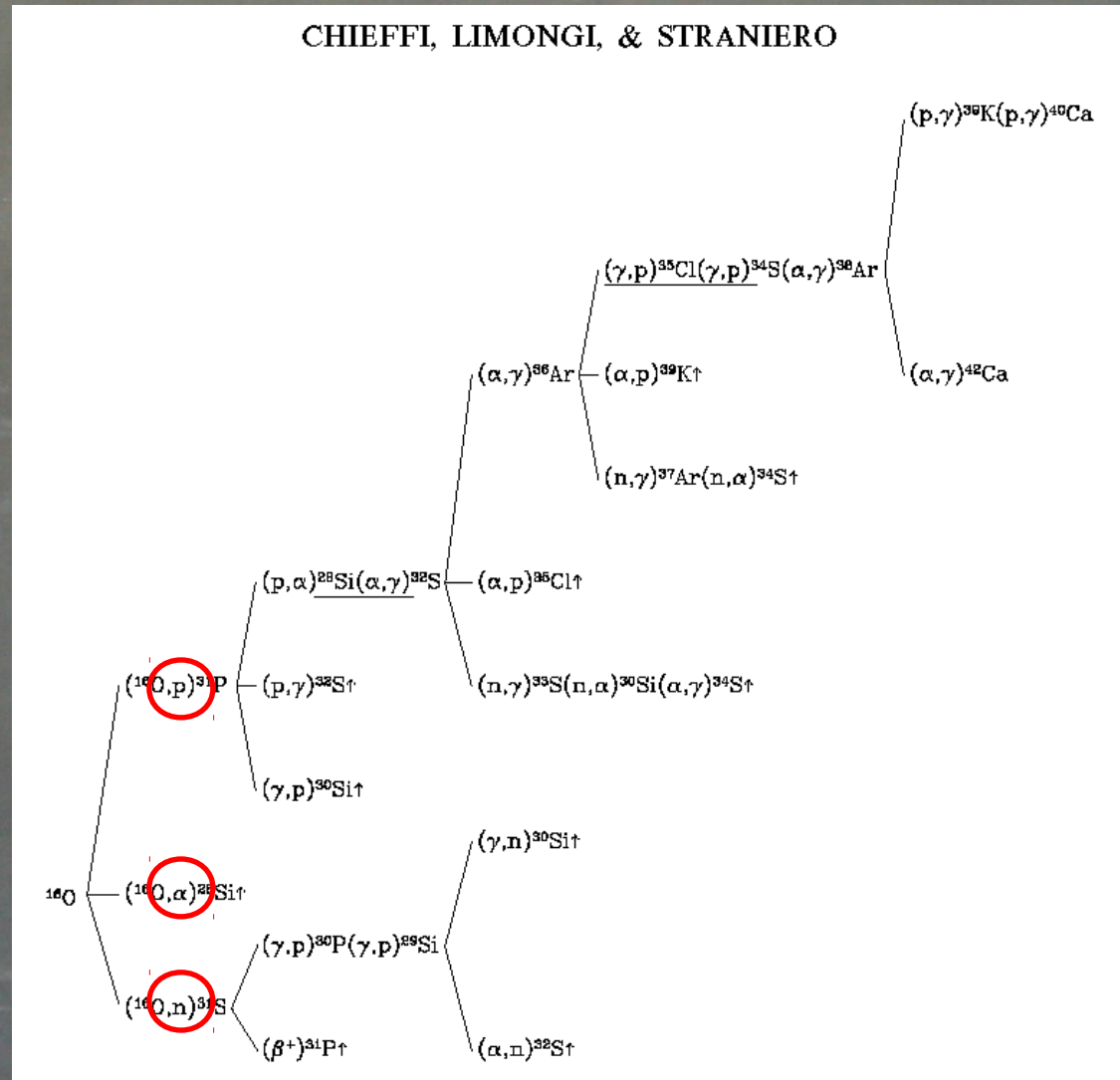
(The O burning products will be fully reprocessed by the passage of the shock wave)





# Just the main processes in ...

## O burning

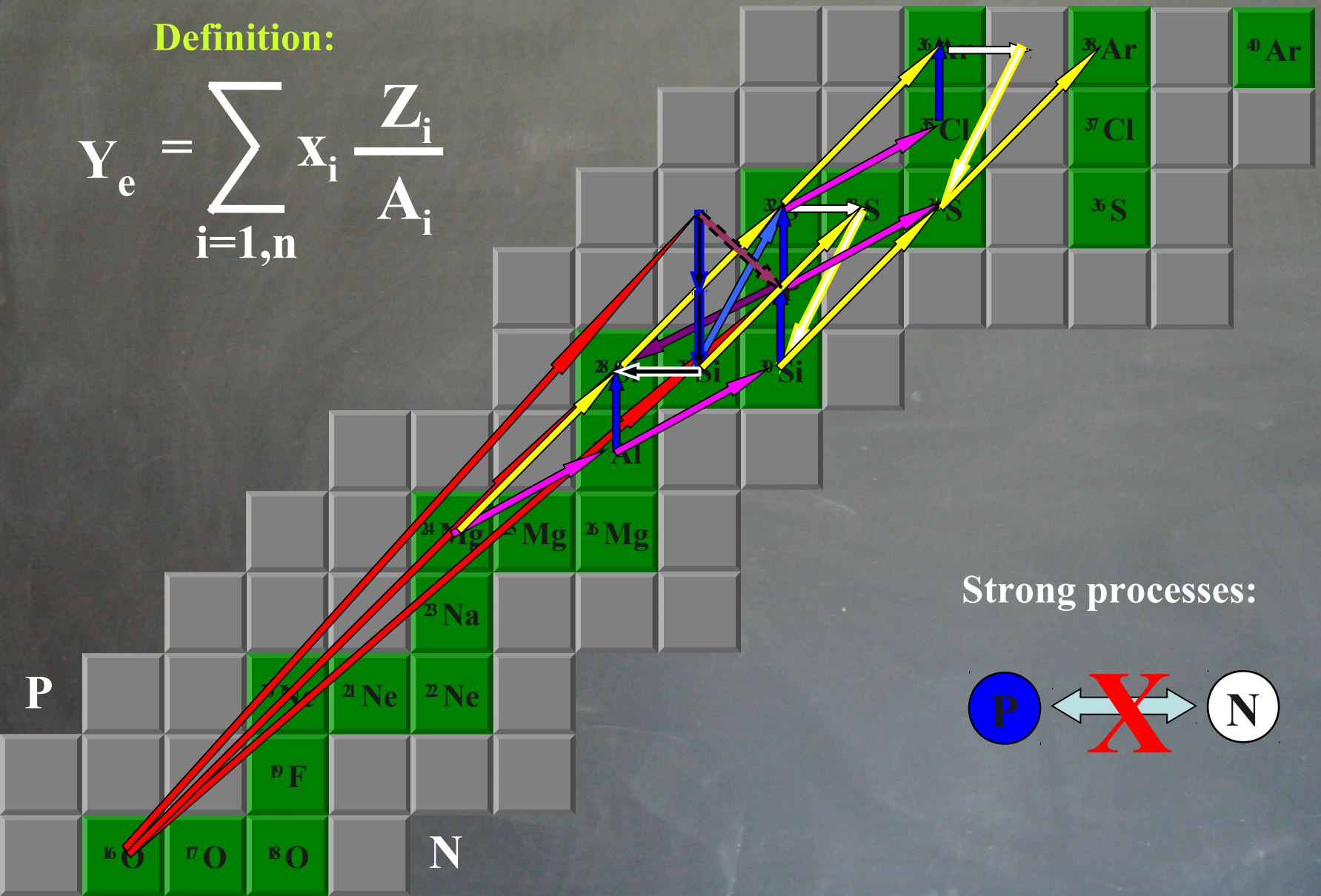




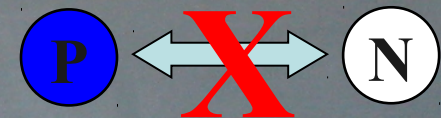
# neutronization

Definition:

$$Y_e = \sum_{i=1,n} x_i \frac{Z_i}{A_i}$$



Strong processes:

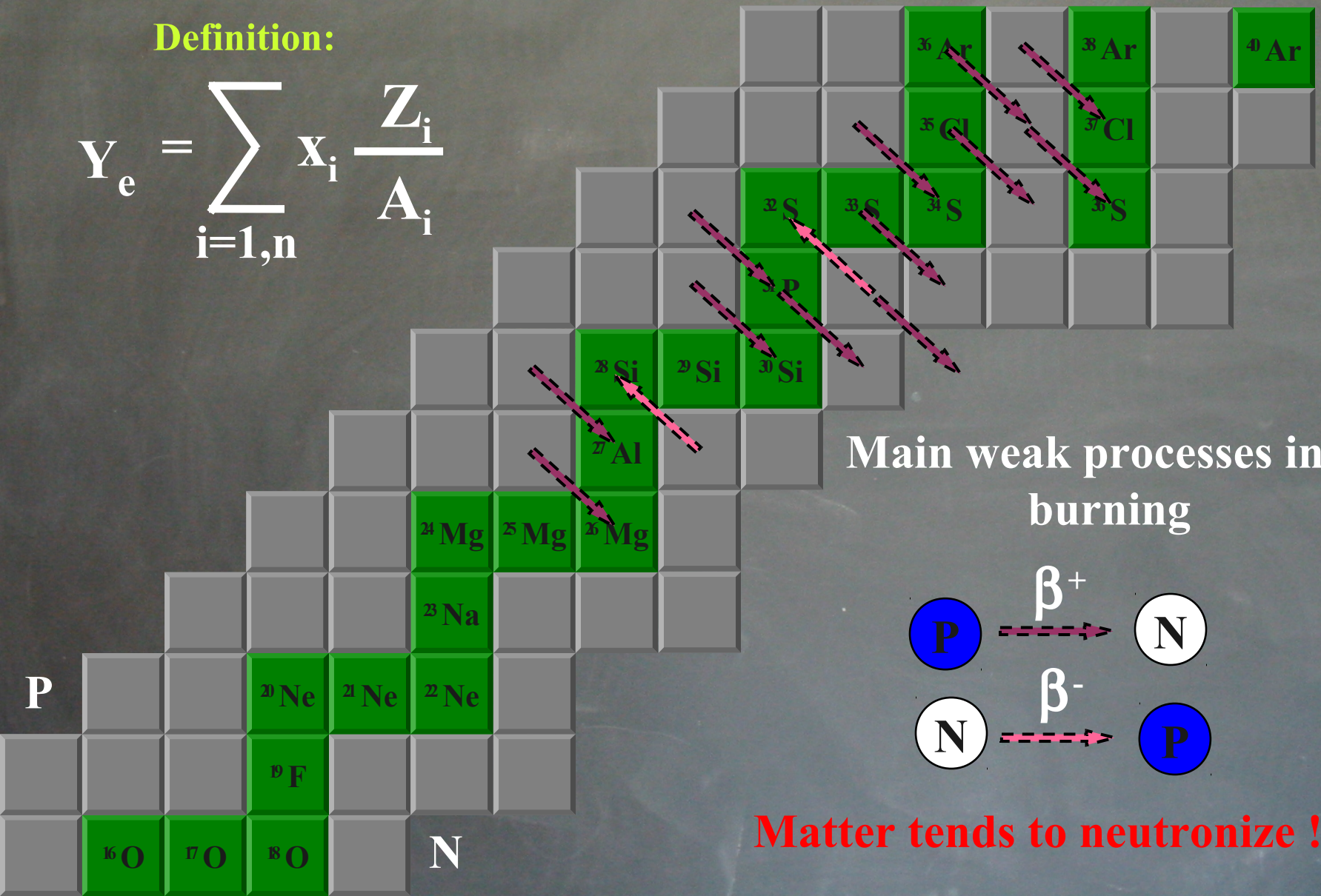




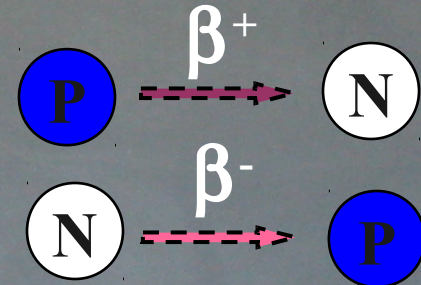
# neutronization

Definition:

$$Y_e = \sum_{i=1,n} x_i \frac{Z_i}{A_i}$$



Main weak processes in O burning



Matter tends to neutronize !

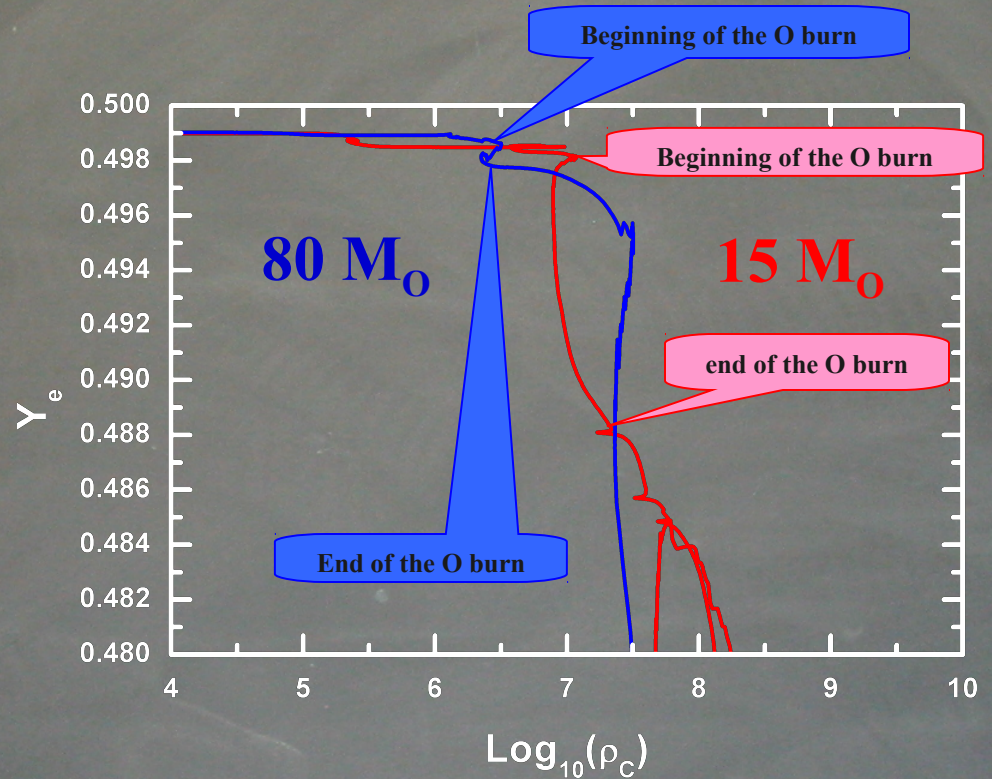


# neutronization

**Definition:**

$$Y_e = \sum_{i=1,n} x_i \frac{Z_i}{A_i}$$

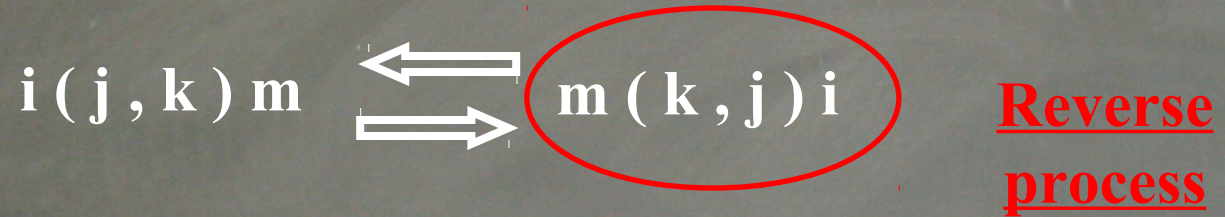
Degree of neutronization depends on the initial mass (actually on CO core mass)



**RULE:** The smaller the  $M_{\text{CO}}$  the higher the degree of neutronization at the end of the central O burning.



## Beyond the O burning



$R_{ij} \rightarrow$  Rate of the  $i(j,k)m$  process

$R_{km} \rightarrow$  Rate of the  $m(k,j)i$  process

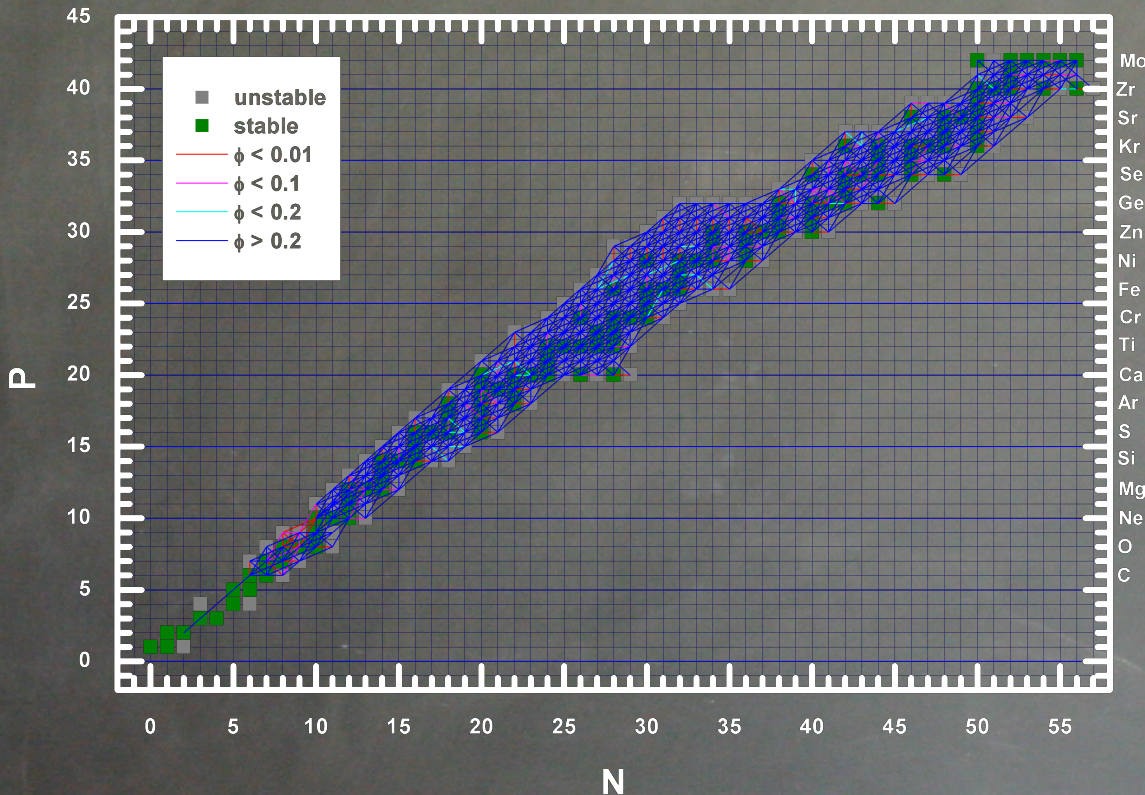
$$\Phi_{ij} = \frac{|R_{ij} - R_{km}|}{\text{Max}(r_{ij}, r_{km})}$$

$\Phi = 0$  means perfect equilibrium

$\Phi = 1$  means one process dominates over the other



# The approach to the Nuclear Statistical Equilibrium



$T=1.9 \text{ BK}$

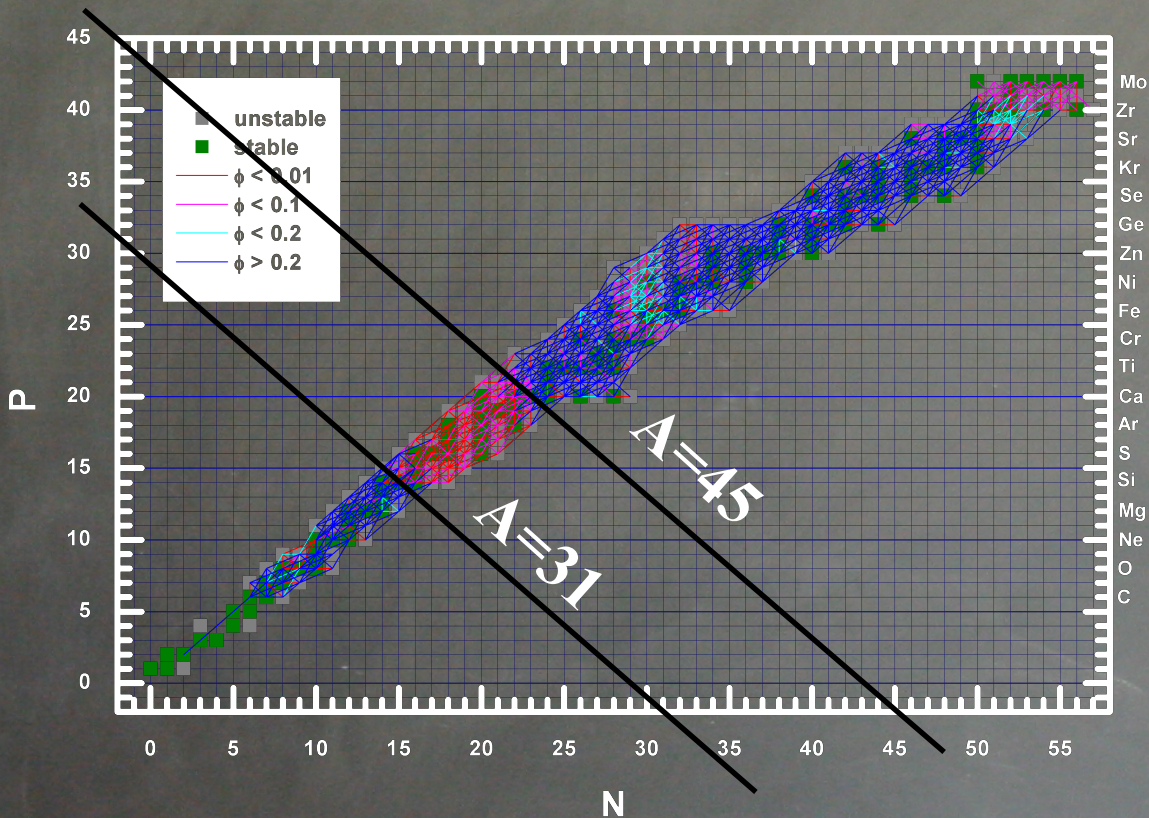
Beginning of the O burning

$Y_e=0.4987$

Almost all the processes  
are far from the  
equilibrium with their  
reverse



# The approach to the Nuclear Statistical Equilibrium



$T=2.7 \text{ BK}$

End of the O burning

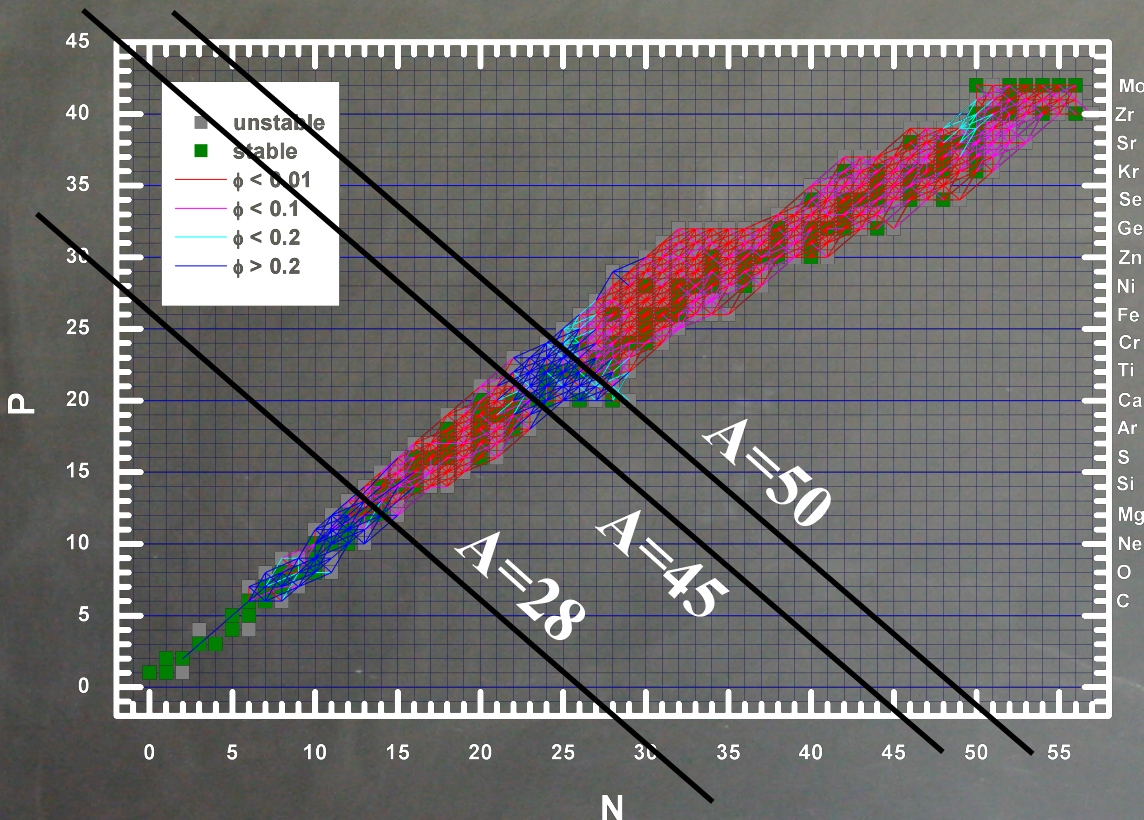
$Y_e=0.4978$

A first cluster forms  
between  $A=31$  and  
 $A=45$

**Definition: a CLUSTER is a group of nuclei connected by processes that are at the equilibrium with their reverse.**



# The approach to the Nuclear Statistical Equilibrium



$T=2.9 \text{ BK}$

A little bit before the Si burning  
 $Y_e=0.4976$

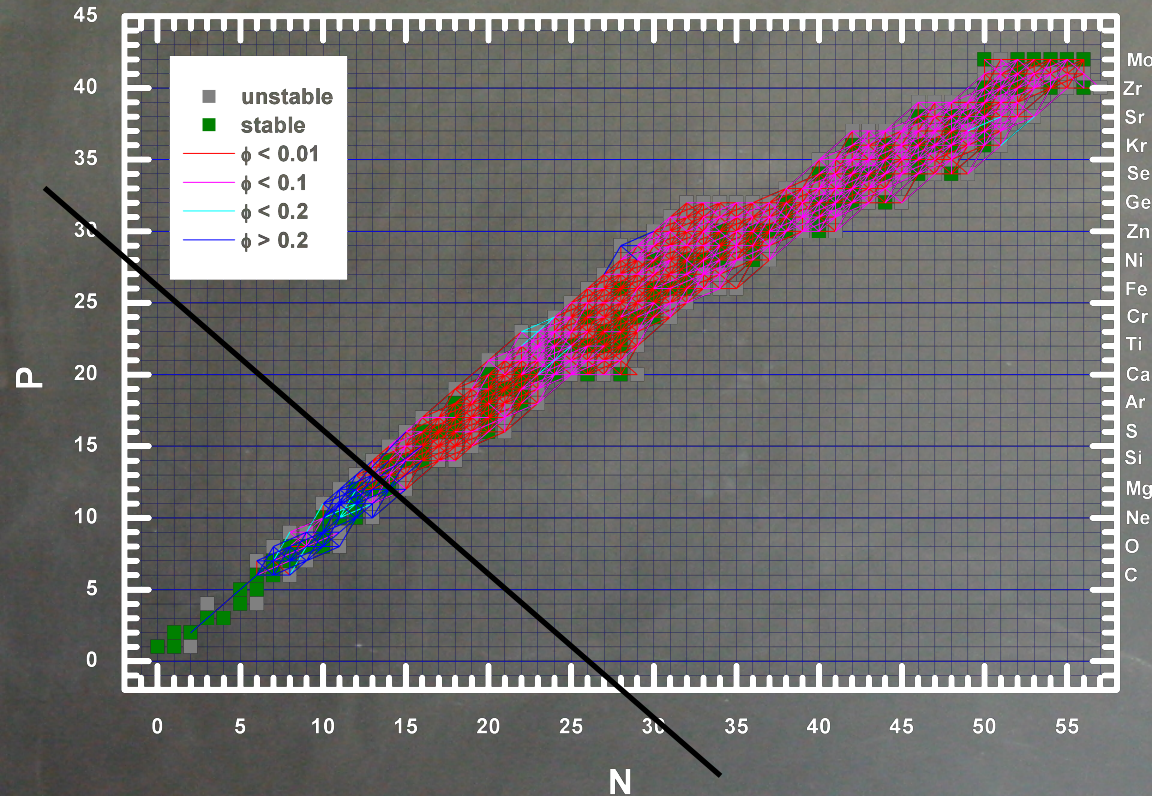
The first cluster extends now  
 between  $A=28$  and  $A=45$   
 but  
 a second one forms at  $A>50$

Within each cluster the abundances of the various nuclei depend on their equilibrium with respect to the sea of  $\alpha$  and  $p$ . Such an equilibrium abundance is determined by an equation that looks like a Saha equation:

$$Y(n,z)=f(\rho, T, \text{a nucleus not in equilibrium})$$



# The approach to the Nuclear Statistical Equilibrium



$T=3.4 \text{ BK}$

Beginning of the Si burning  
 $Y_e=0.4955$

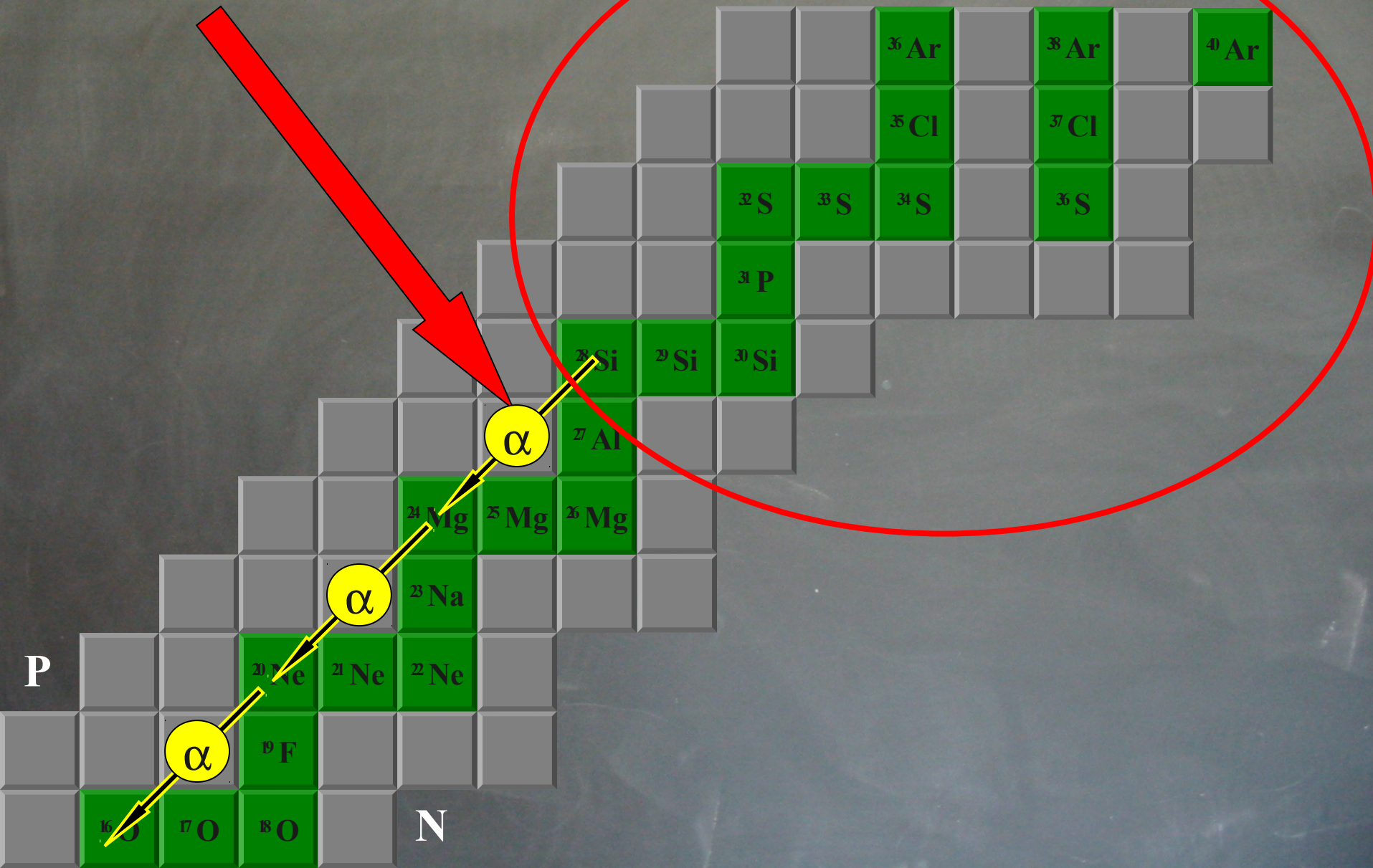
The two clusters begin to  
 merge and form an unique  
 cluster that starts at  $A=28$

$^{28}\text{Si}$  is not at the equilibrium. It is destroyed by the  $\gamma, \alpha$   
 photodisintegration



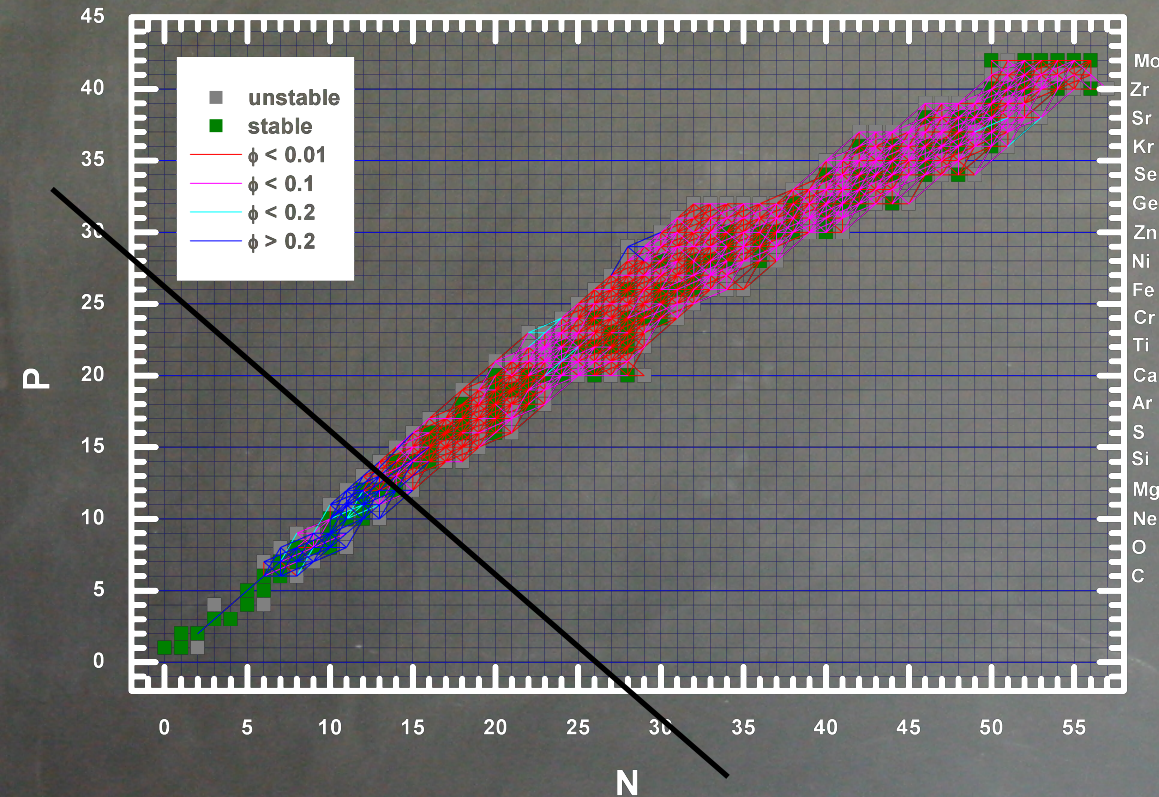
whole photointegration from  $^{28}\text{Si}$  to the  $\alpha$  is in equilibrium and regulates the timescale over which nucleons are liberated (and hence redistributed among the various nuclei)

The diagram illustrates a nucleon ladder with various isotopes. A red arrow points to the  $^{28}\text{Si}$  nucleus, which is the starting point of the path. A red circle encloses the path from  $^{28}\text{Si}$  to  $^{40}\text{Ar}$ . The path is highlighted in green and includes the following isotopes:  $^{28}\text{Si}$ ,  $^{29}\text{Al}$ ,  $^{30}\text{Si}$ ,  $^{31}\text{P}$ ,  $^{32}\text{S}$ ,  $^{33}\text{S}$ ,  $^{34}\text{S}$ ,  $^{35}\text{Cl}$ ,  $^{36}\text{Cl}$ ,  $^{36}\text{Ar}$ ,  $^{37}\text{Ar}$ , and  $^{40}\text{Ar}$ . A yellow circle labeled  $\alpha$  is positioned near the  $^{28}\text{Si}$  nucleus, and a yellow arrow points from it to the  $^{28}\text{Si}$  nucleus.





# The approach to the Nuclear Statistical Equilibrium



$T=3.4 \text{ BK}$

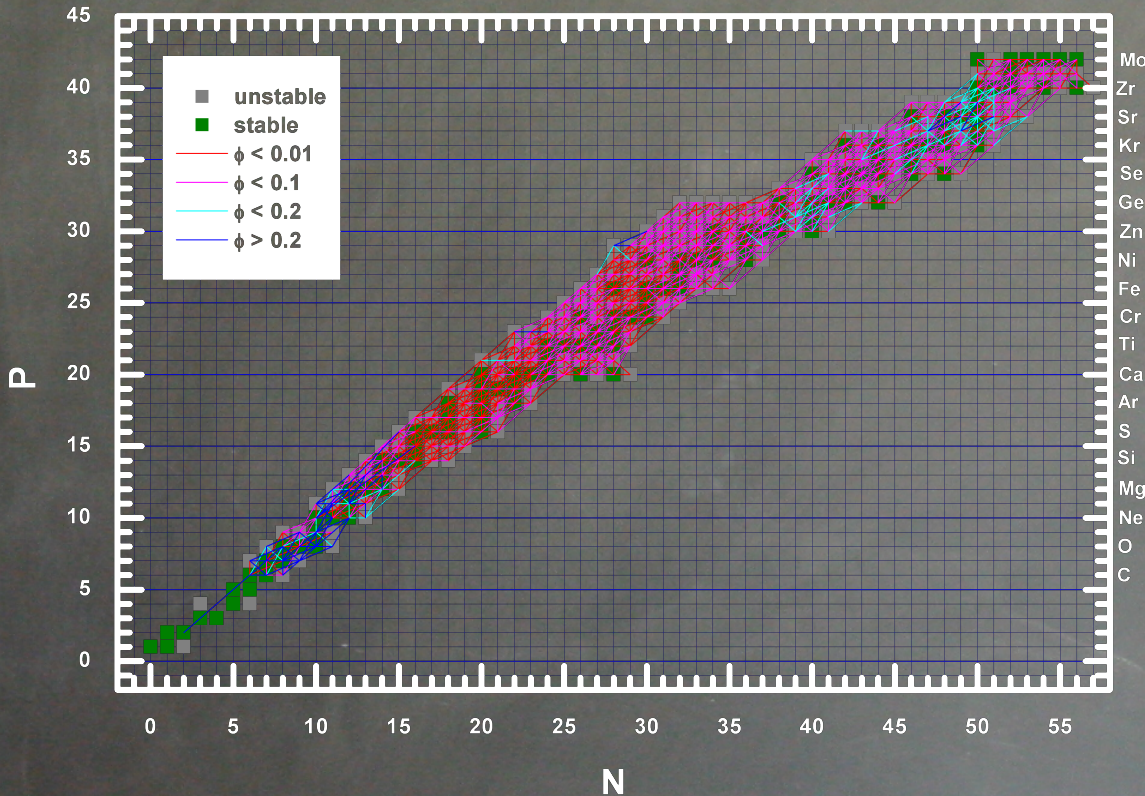
Beginning of the Si burning  
 $Y_e=0.4955$

The two clusters begin to  
 merge and form an unique  
 cluster that starts at  $A=28$

$^{28}\text{Si}$  is not at the equilibrium. It is destroyed by the  $\gamma, \alpha$   
 photodisintegration



# The approach to the Nuclear Statistical Equilibrium



$T=4.1 \text{ BK}$

End of the Si burning

$Y_e=0.4780$

Nuclei with  $A < 28$  do not reach the equilibrium

Most of the matter located in the nucleus(i) that has(ve) the highest binding energy for the  $Y_e$  present at the moment. Remember that the weak processes are not at the equilibrium and must be taken into account explicitly!



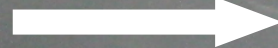
**At 5 BK full Nuclear Statistical equilibrium is attained**

The abundances of the various nuclei are governed by a set of equations of this kind:

$$Y(n, z) = f(\rho, T) \cdot e^{\frac{-Q(n, z)}{KT}} \cdot Y_p^z \cdot Y_n^n$$

The system is closed by the conditions:

Mass conservation



$$\frac{\sum Y_i \cdot A_i}{\sum Y_i} = 1$$

Electron mole number  
conservation

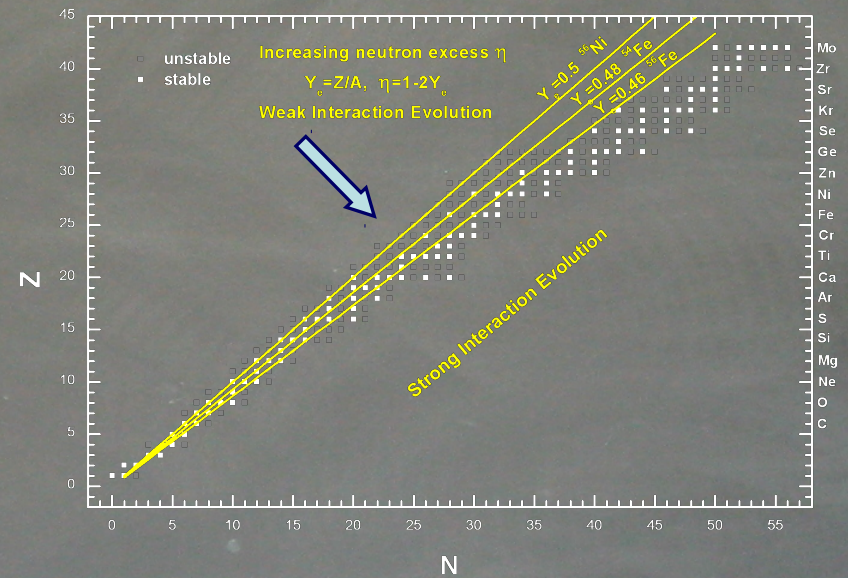
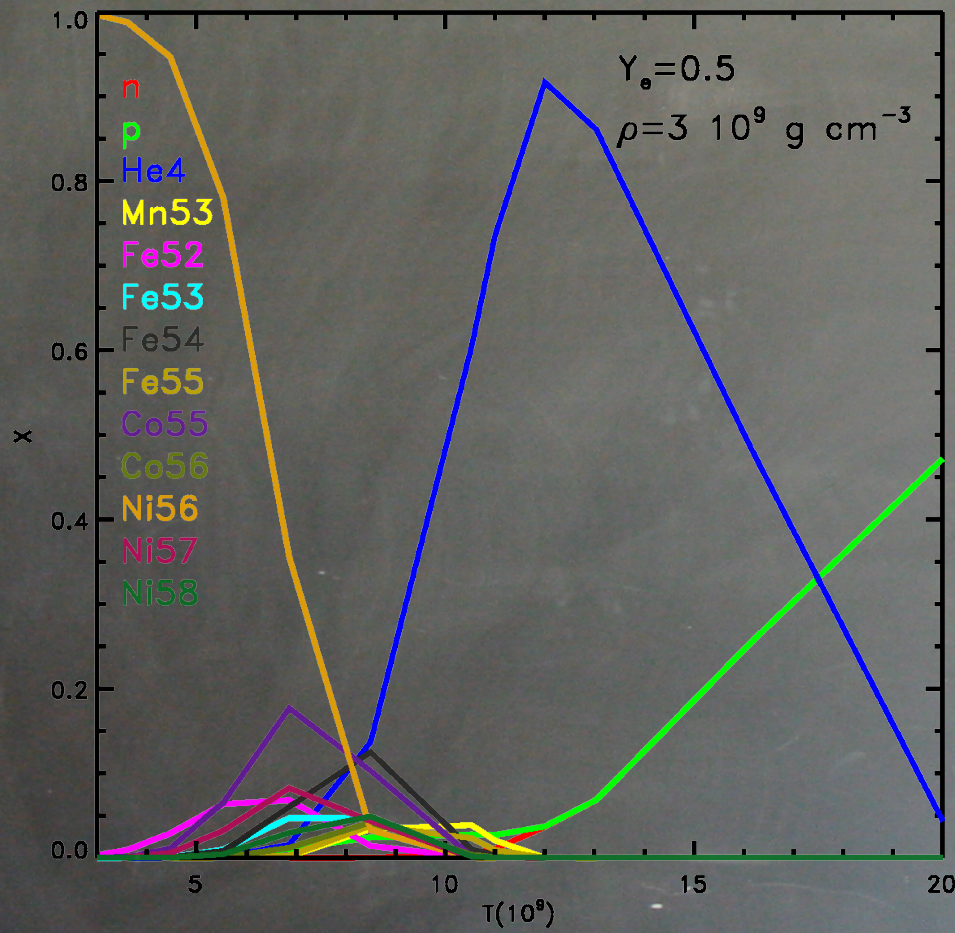


**Y<sub>e</sub> = constant (at each time)**

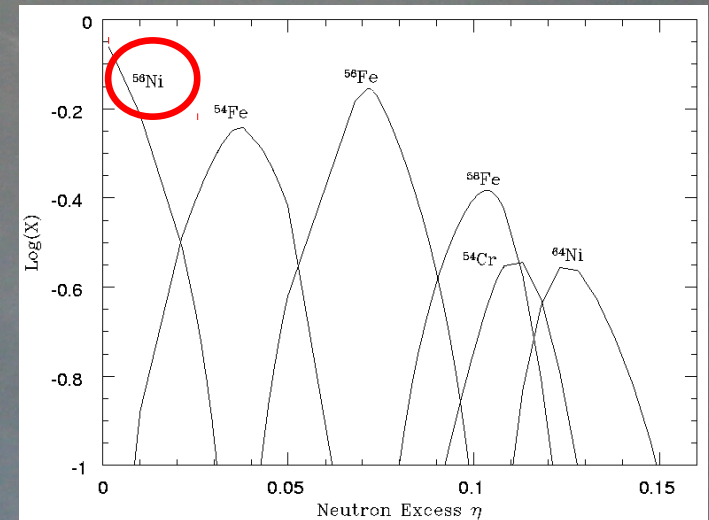
**The abundances of all the nuclei depend only on  $\rho$ , T and Y<sub>e</sub>**



# Most abundant elements in NSE conditions as a function of the temperature



T = 5 · 10<sup>9</sup> K ρ = 10<sup>8</sup> g/cm<sup>3</sup>

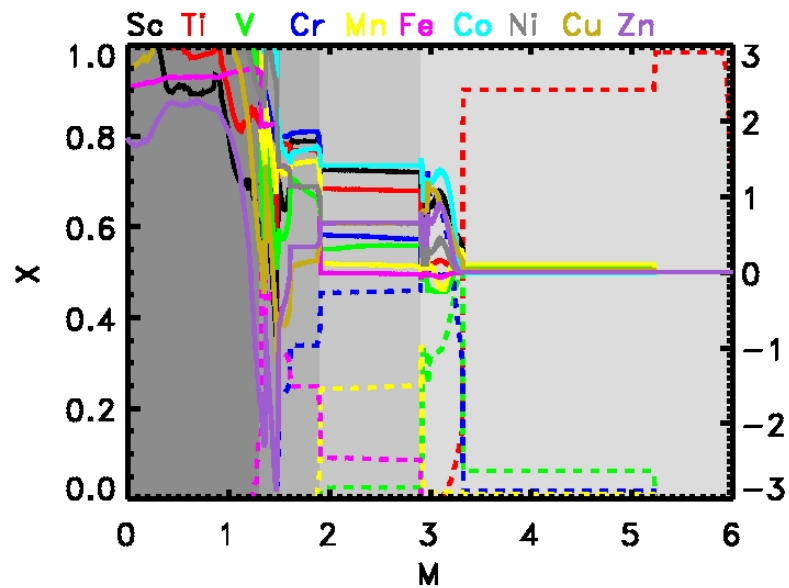
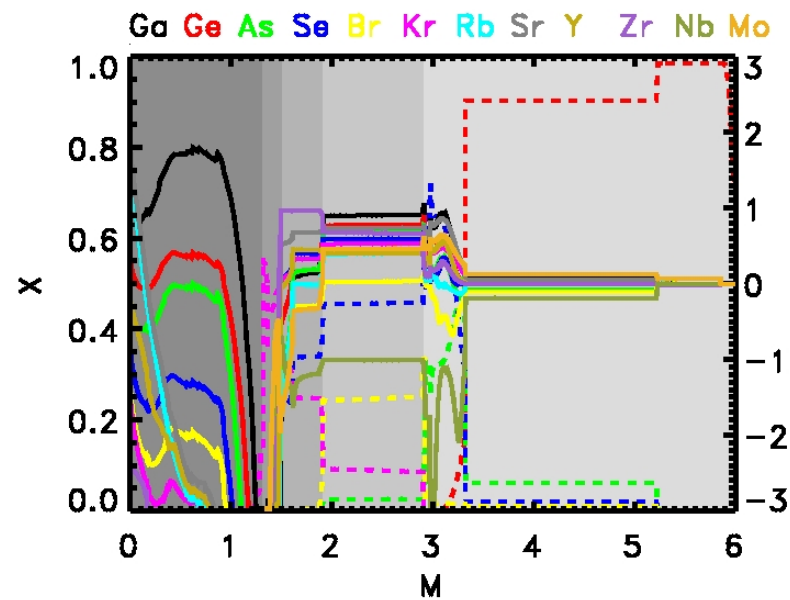
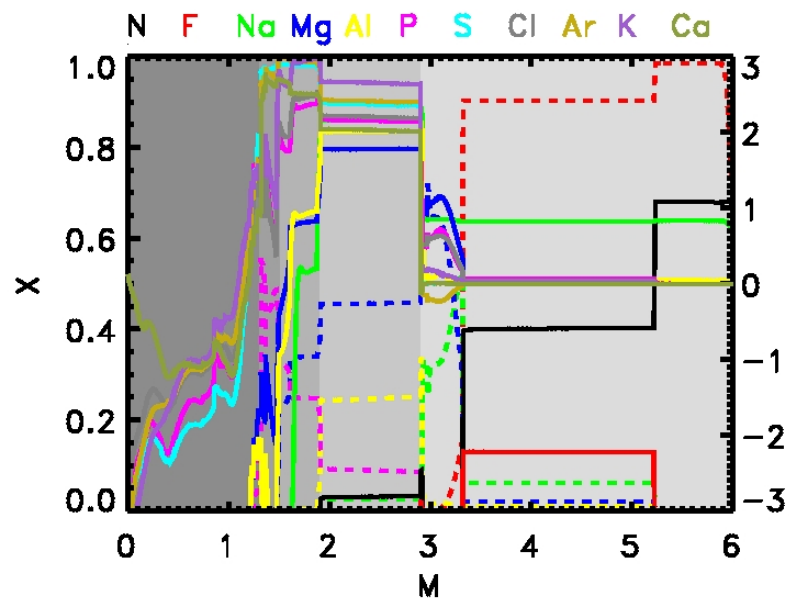




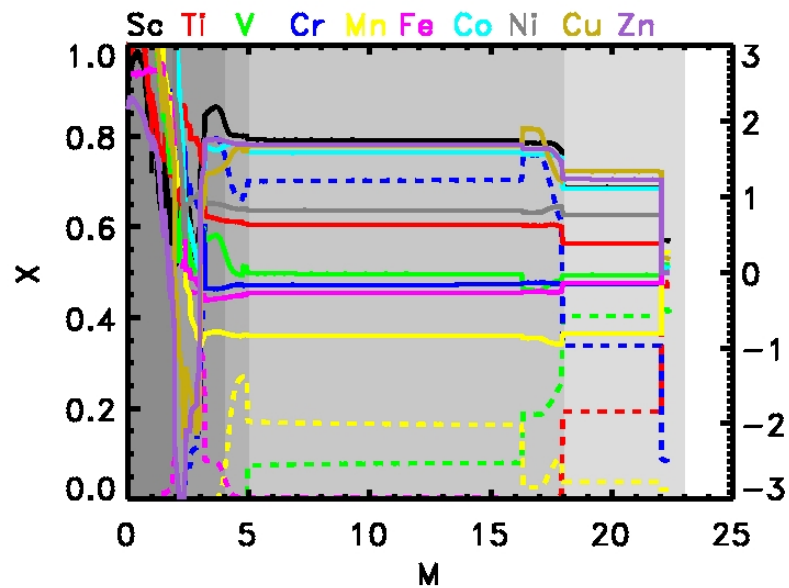
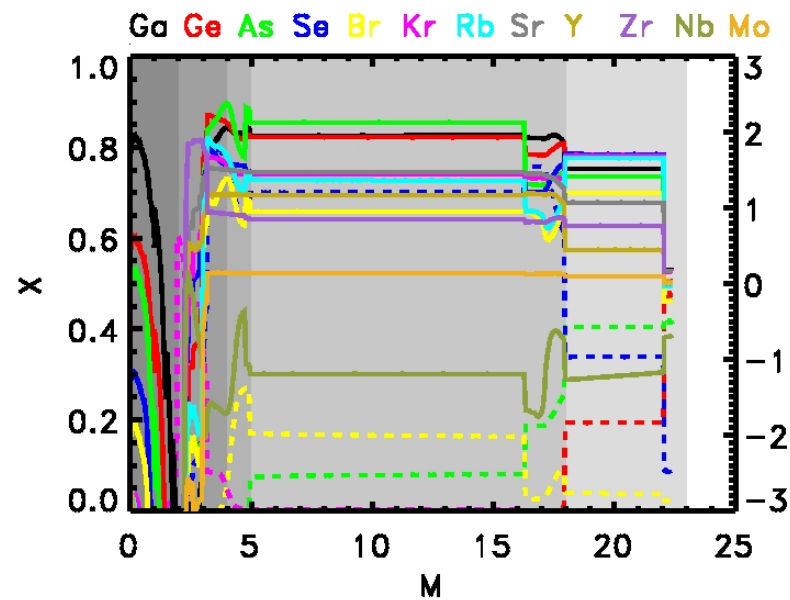
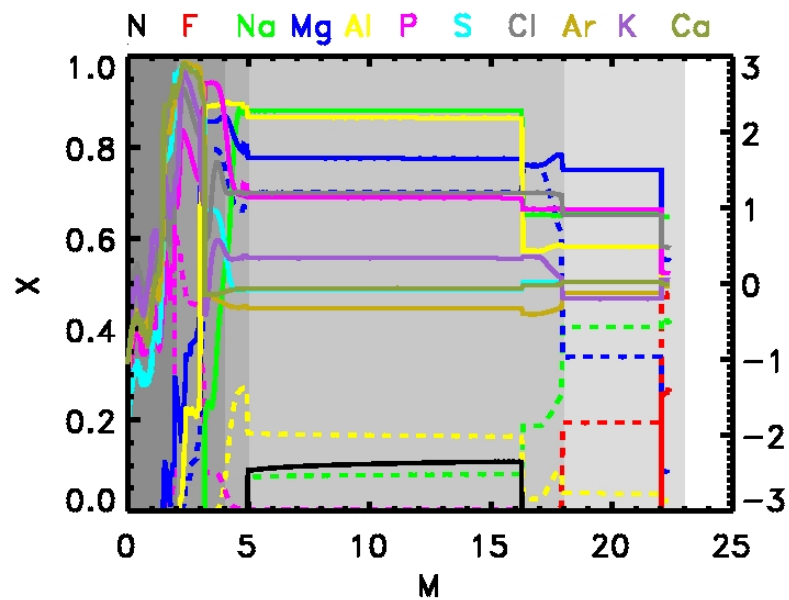
**Trailer time!**

**O & Si burnings movie**

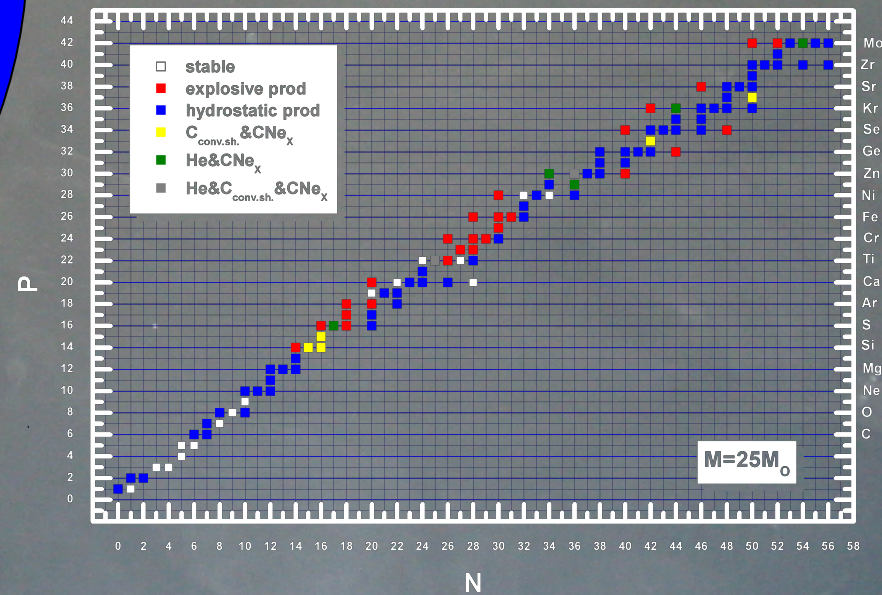
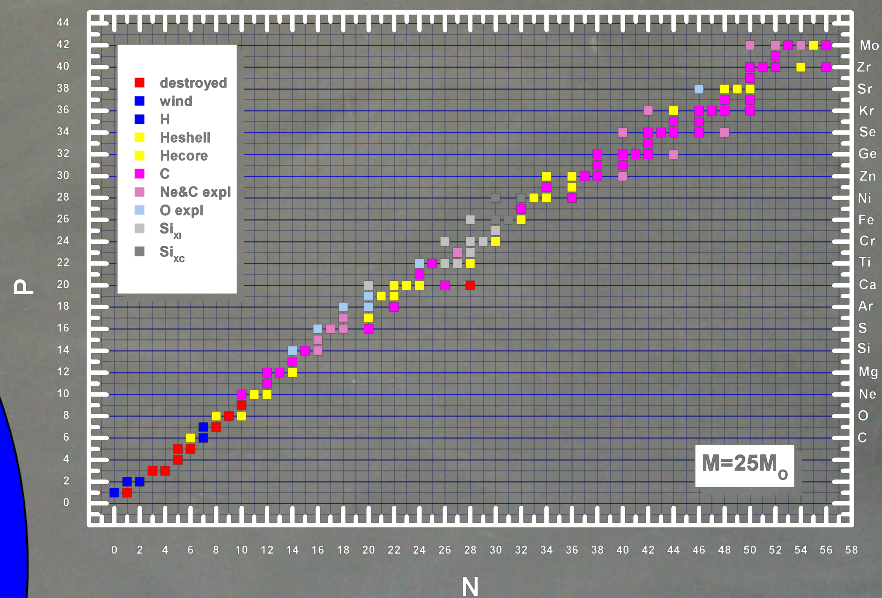
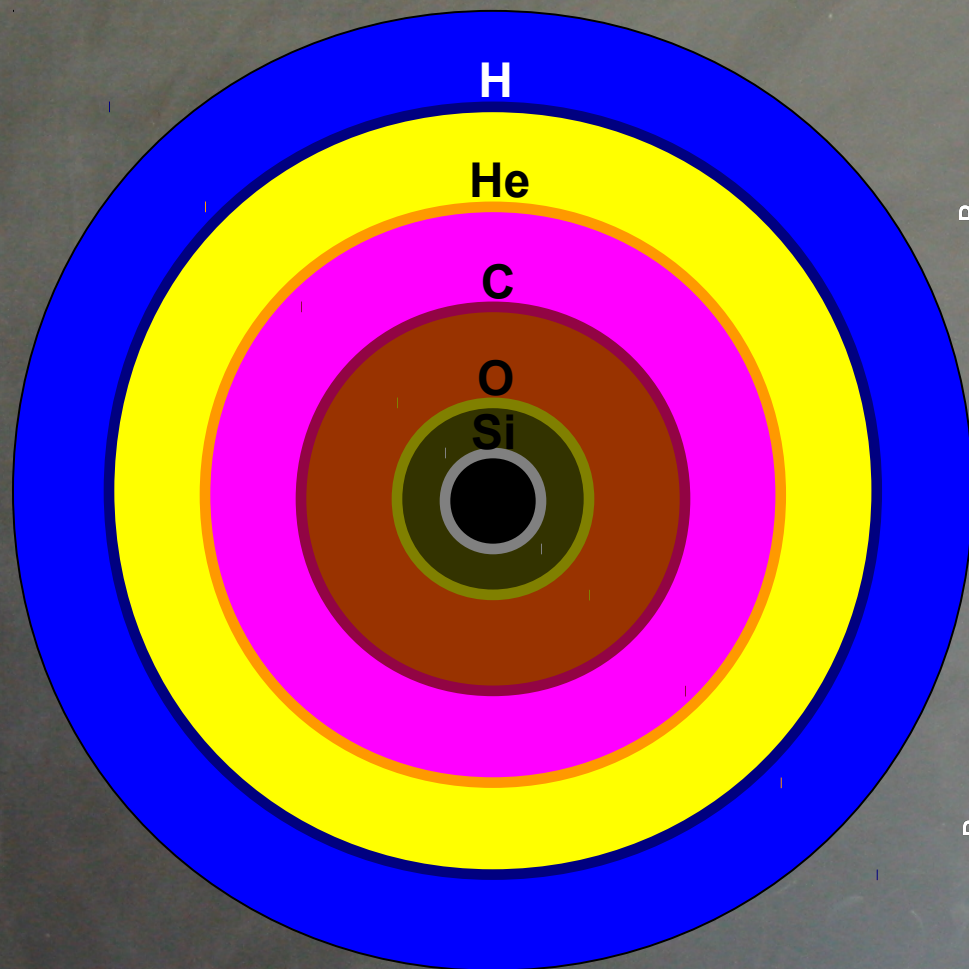




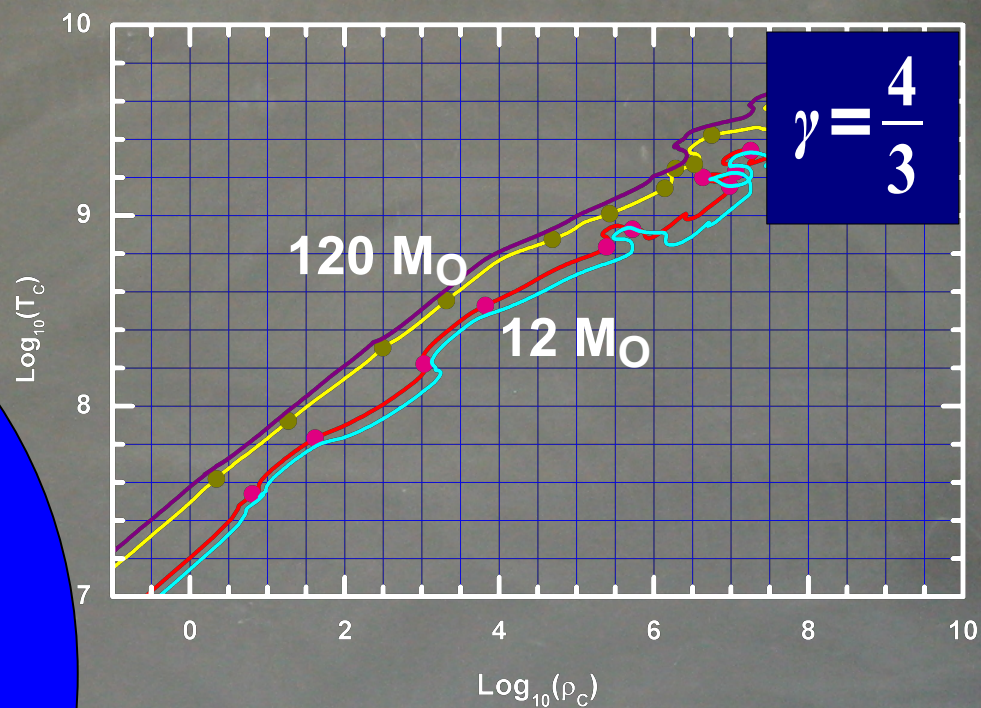
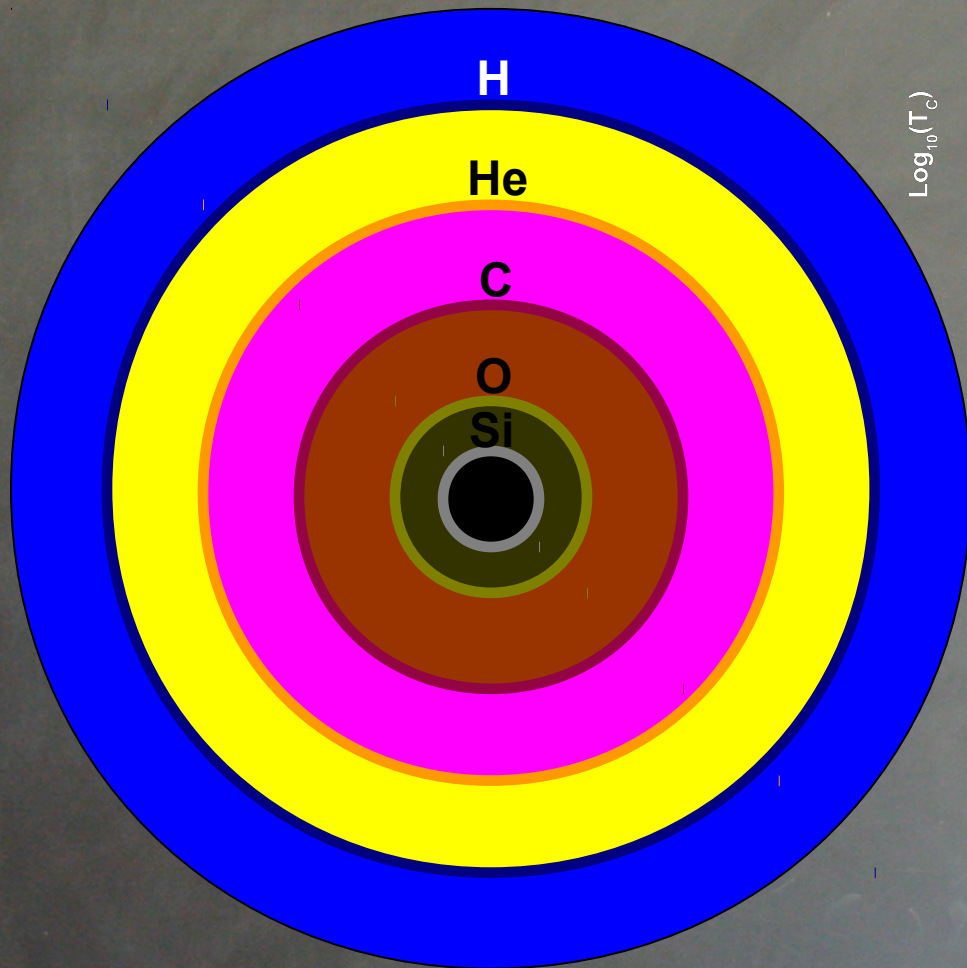












**Virial theorem**

$$3(\gamma - 1)U + \Omega = 0$$

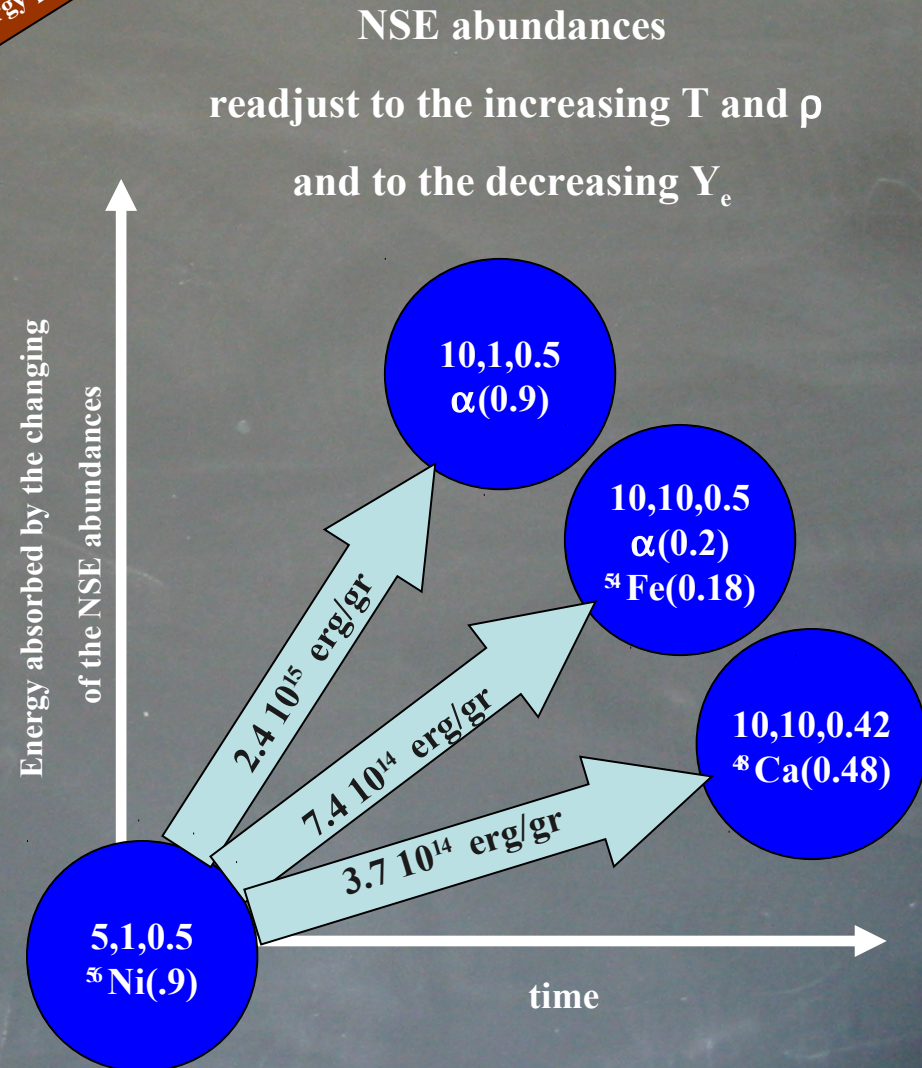
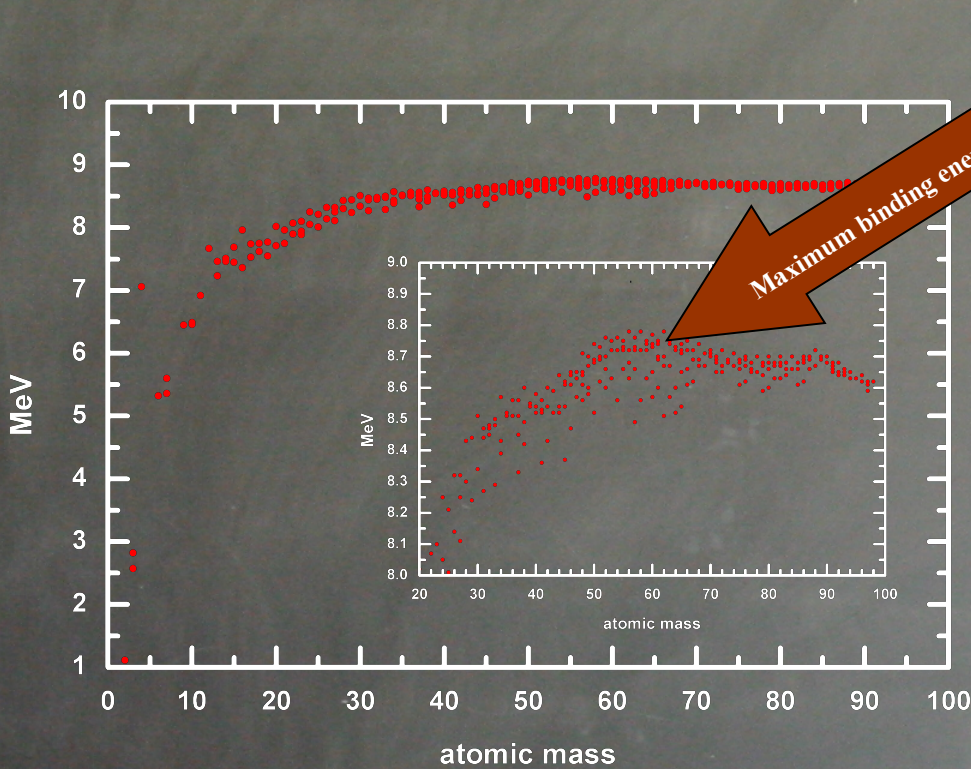
$$U + \Omega \equiv E_{TOT} = 0$$

$$\Delta E_{TOT} \equiv \cdot$$

NO delay is required for a contraction,  
the structure is only marginally stable



# What happens to the inner core after the central Si burning?





Characteristic masses

